



# AROME Ensemble-Variational 3D/ 4D-EnVar under OOPS

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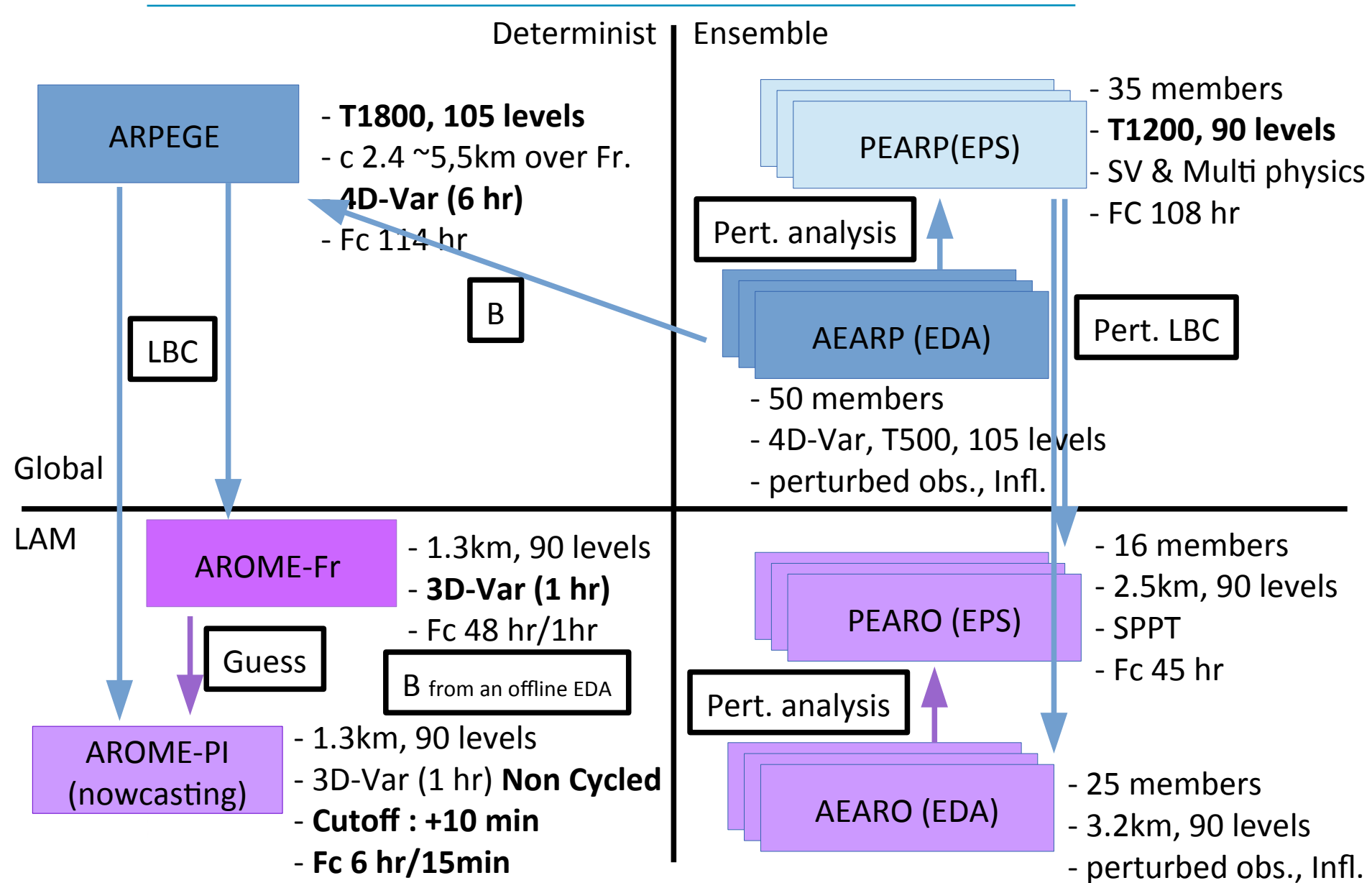
42nd EWGLAM and 27th SRNWP Meeting  
4 septembre 2020

# plan

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- **Introduction**
- **Summary of 3D-envar developments**
- **4D-envar ongoing works**

# Meteo-France NWP system



# OOPS : Object -Oriented Programing System

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## Next major evolution of the DA systems : towards Envar scheme

### Using OOPS :

- project done at ECMWF in collaboration with Météo-France and LAM partners
- renovation of common data assimilation codes in order to enable the development of new algorithms and ease maintenance
- object-oriented design, upper level code in C++
- important refactoring of the IFS-Arpege-LAM FORTRAN codes
- main part of the coding effort now completed

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- **Introduction**
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# Prototype Envar sous OOPS

DA in AROME is performed using an incremental VAR formulation in 3D

$$J(\delta x) = \frac{1}{2} \delta x^T \mathbf{B}^{-1} \delta x + \frac{1}{2} (d - \mathbf{H}\delta x)^T \mathbf{R}^{-1} (d - \mathbf{H}\delta x)$$

- **Operationally, hourly-cycled 3DVar are performed with** : Brousseau et al. 2016

$\mathbf{B} = \overline{\mathbf{B}}$  is climatological and modeled following Berre (2000)

$$\delta x = \overline{\mathbf{B}}^{1/2} \chi \text{ with } \chi = (\zeta, \eta_u, (T, P_s)_u, q_u)$$

⇒ No flow dependencies : Homogeneous correlations, static variances

- **EnVar configurations have been implemented in OOPS :**

- Full ensemble :  $\mathbf{B} = \tilde{\mathbf{B}}_e$

- Hybrid :  $\mathbf{B} = \beta_c \overline{\mathbf{B}} + \beta_e \tilde{\mathbf{B}}_e$

$$\delta x = \mathbf{B}g$$

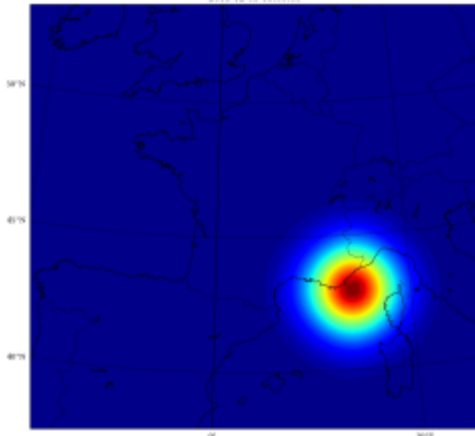
with a B-preconditioning :  $g = (U, V, (T, P_s), q)$

# 3DEnvar : Montmerle et al. 2018

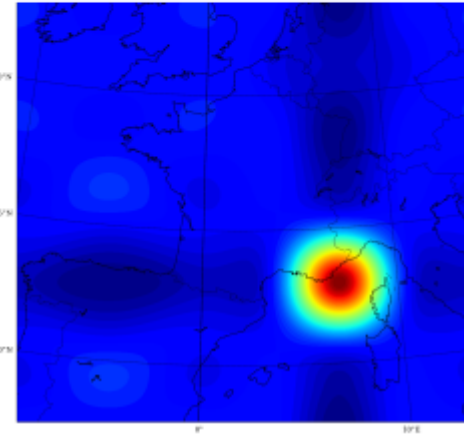
## Experiments at 3,8km in a 3h cycle :

- comparison of spectral/spacial localisation

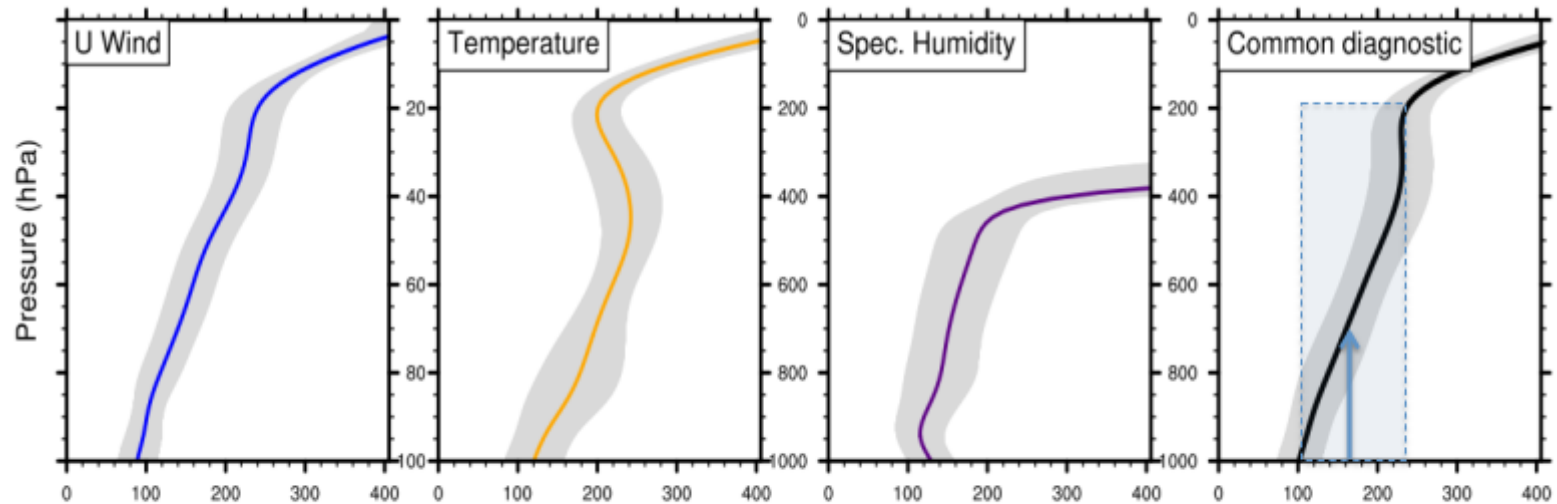
Spatial (michel 2012) : recursive filters of (Purser, 2003)



Spectral : inverse bi-Fourier transforms



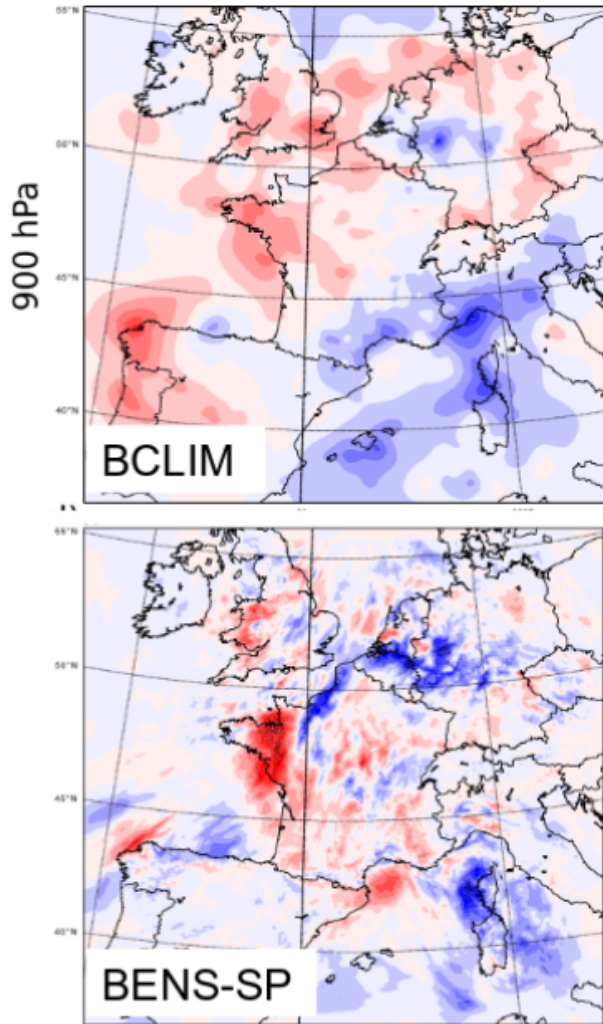
- diagnostic (Ménétrier 2015) and investigation on localisation length-scales



# 3DEnvar : Montmerle et al. 2018

(by Thibaut M.)

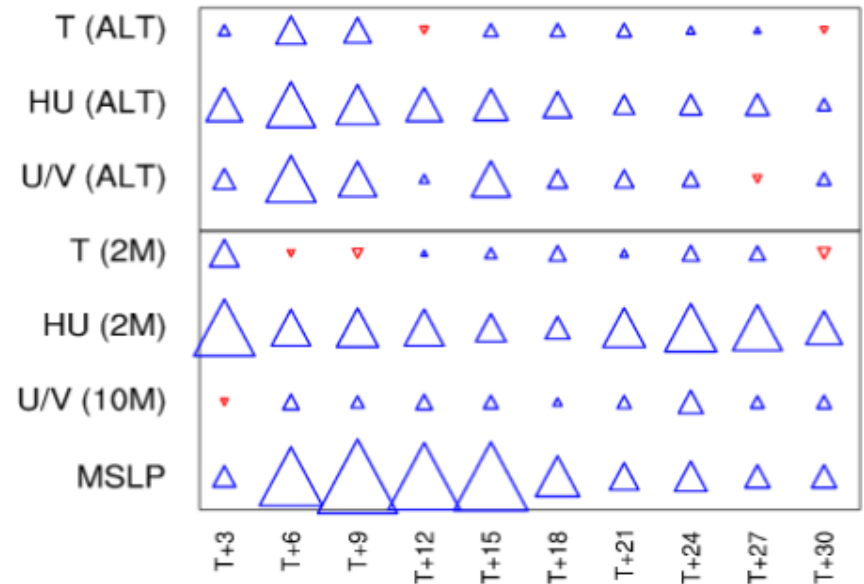
- Montmerle et al. 2018 QJRMS : 3,8km in a 3-h cycle : encouraging results



*Inc(T)*  
6<sup>th</sup> of



ScoreCard BENS-GP vs. BCLIM  
20160206-20160310: HH12



Total NWP index change (altitude) : +1.4 %

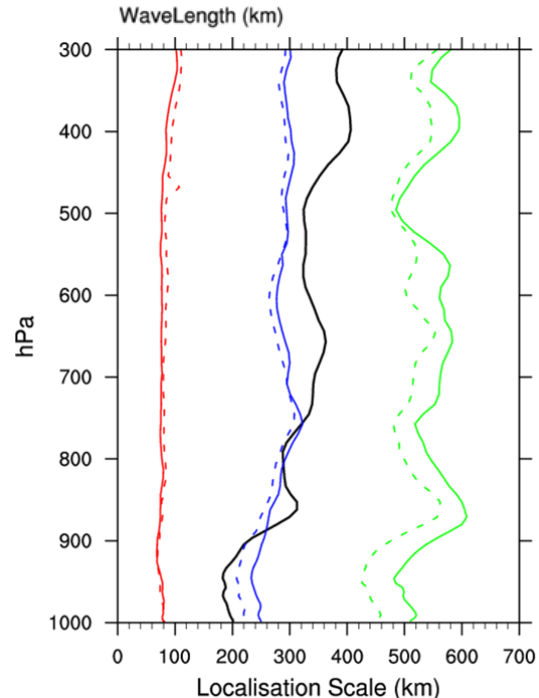
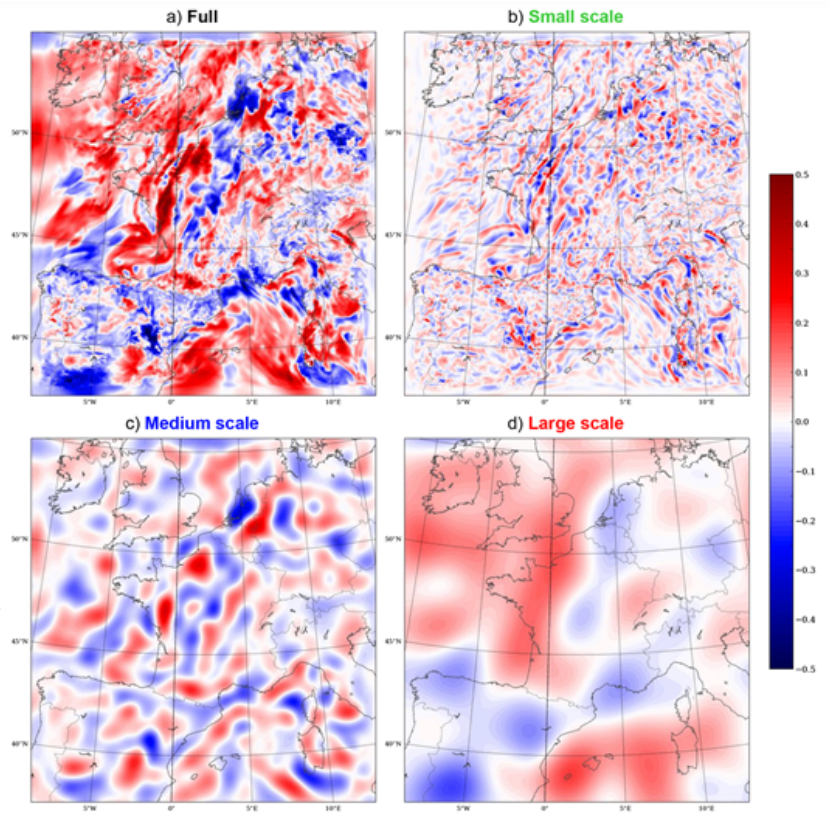
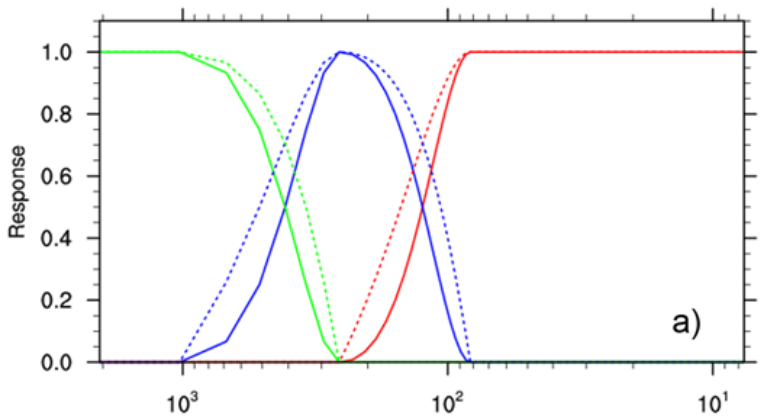
Total NWP index change (surface) : +1.9 %





# Scale-dependent localisation (Caron et al. 2019)

Wave band decomposition of the background error covariances :



Scale dependent localisation

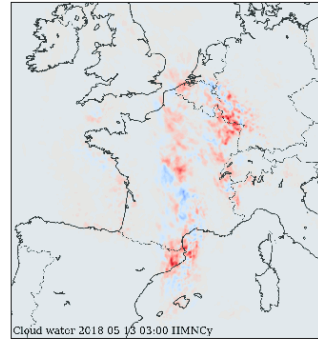
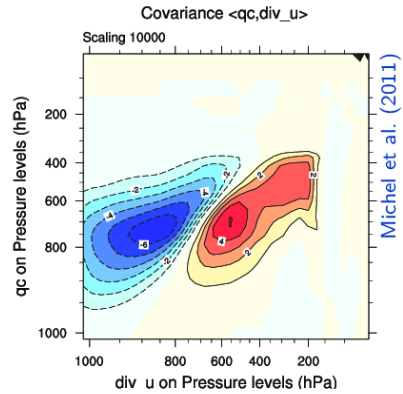
# hydrometeors analysis (M. Destouches PhD)

Increments in standard variables



Cross-covariances with hydrometeors

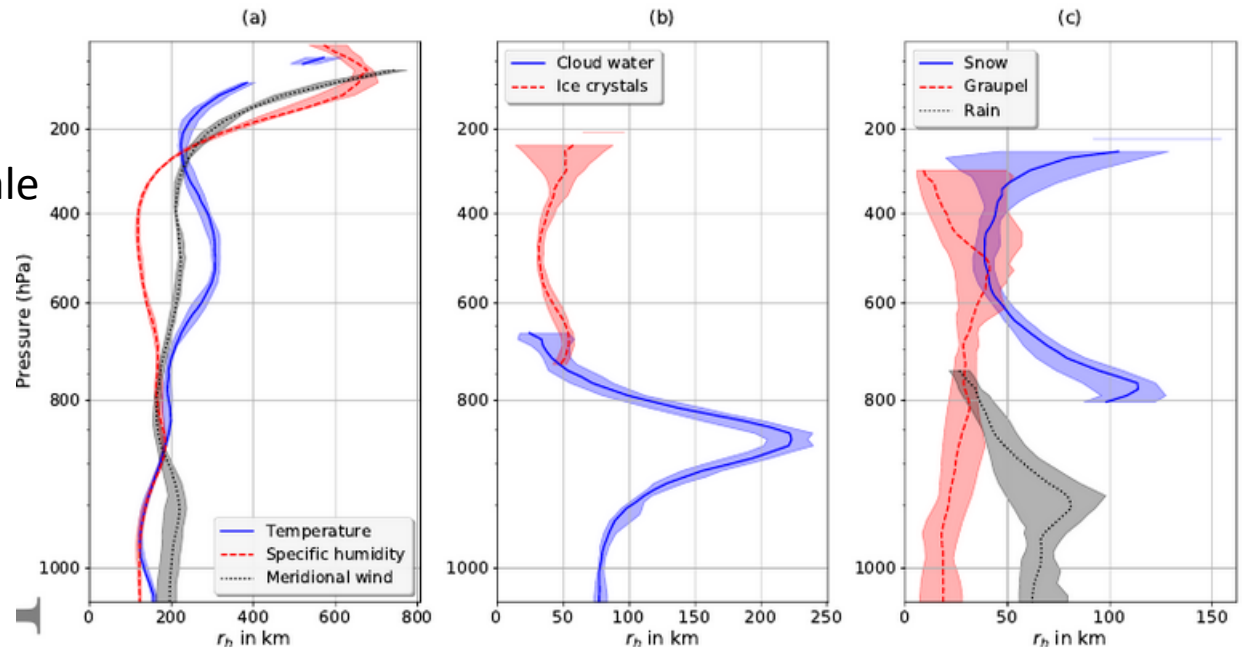
Hydrometeor increments



- allows standard observations to modify the hydrometeors fields according to the background error cross-correlations deduced from the EDA :

Hydrometeors localisation Scale

Destouches et al. 2020



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# 4DVar

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- toward a full 4DVar system :

$$\text{3D-Var : } J(\delta\mathbf{x}) = \frac{1}{2}(\delta\mathbf{x})^T \mathbf{B}^{-1}(\delta\mathbf{x}) + \frac{1}{2}(\mathbf{d} - \mathbf{H}\delta\mathbf{x})^T \mathbf{R}^{-1}(\mathbf{d} - \mathbf{H}\delta\mathbf{x})$$

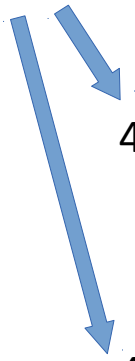


$$\text{4D-Var : } J(\delta\mathbf{x}) = \frac{1}{2}(\delta\mathbf{x})^T \mathbf{B}^{-1}(\delta\mathbf{x}) + \frac{1}{2} \sum_{i=0}^K (\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{0 \rightarrow i} \delta\mathbf{x})^T \mathbf{R}_i^{-1} (\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{0 \rightarrow i} \delta\mathbf{x})$$

# 4DVar

- toward a full 4DVar system :

3D-Var :  $J(\delta \mathbf{x}) = \frac{1}{2}(\delta \mathbf{x})^T \mathbf{B}^{-1}(\delta \mathbf{x}) + \frac{1}{2}(\mathbf{d} - \mathbf{H}\delta \mathbf{x})^T \mathbf{R}^{-1}(\mathbf{d} - \mathbf{H}\delta \mathbf{x})$



4D-Var :  $J(\delta \mathbf{x}) = \frac{1}{2}(\delta \mathbf{x})^T \mathbf{B}^{-1}(\delta \mathbf{x}) + \frac{1}{2} \sum_{i=0}^K (\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{0 \rightarrow i} \delta \mathbf{x})^T \mathbf{R}_i^{-1}(\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{0 \rightarrow i} \delta \mathbf{x})$

4DVar :  $J(\underline{\delta \mathbf{x}}) = \frac{1}{2}(\underline{\delta \mathbf{x}})^T \underline{\mathbf{B}}^{-1}(\underline{\delta \mathbf{x}}) + \frac{1}{2}(\underline{\mathbf{d}} - \underline{\mathbf{H}}\underline{\delta \mathbf{x}})^T \underline{\mathbf{R}}^{-1}(\underline{\mathbf{d}} - \underline{\mathbf{H}}\underline{\delta \mathbf{x}})$

Desroziers et al. 2014



$$\underline{\delta \mathbf{x}} = \begin{pmatrix} \delta \mathbf{x}_0 \\ \delta \mathbf{x}_1 \\ \vdots \\ \delta \mathbf{x}_K \end{pmatrix}$$

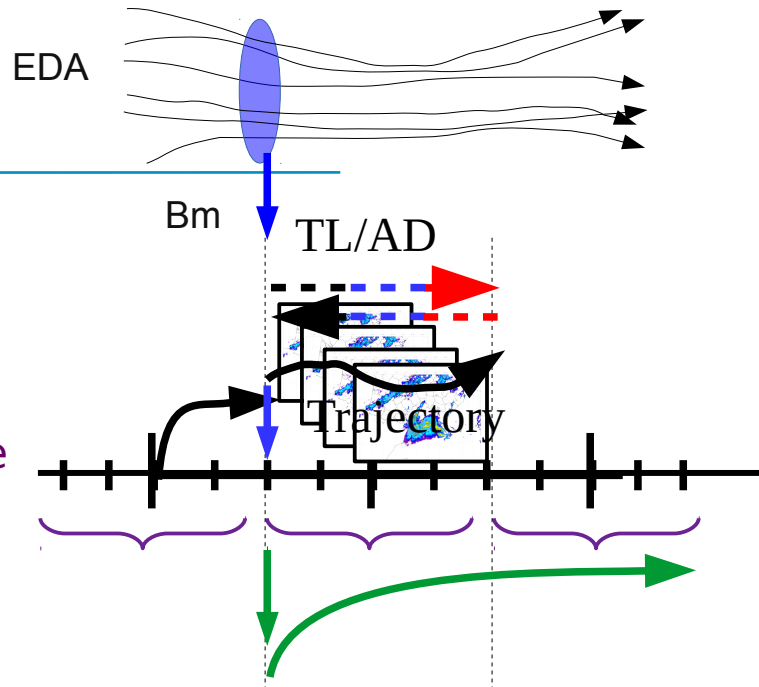
$$\underline{\mathbf{B}} = \underline{\tilde{\mathbf{B}}}^e = \begin{pmatrix} \tilde{\mathbf{B}}_{0,0}^e & \tilde{\mathbf{B}}_{0,1}^e & \cdots & \tilde{\mathbf{B}}_{0,K}^e \\ \tilde{\mathbf{B}}_{1,0}^e & \tilde{\mathbf{B}}_{1,1}^e & & \tilde{\mathbf{B}}_{1,K}^e \\ \vdots & & \ddots & \\ \tilde{\mathbf{B}}_{K,0}^e & \cdots & & \tilde{\mathbf{B}}_{K,K}^e \end{pmatrix}$$



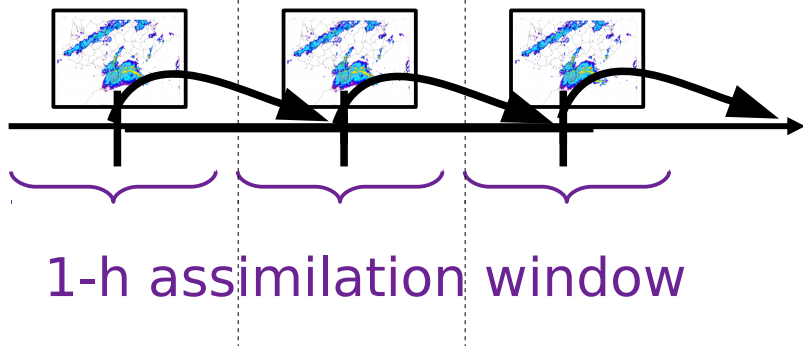
# 4DEnvar

- Operational AROME-Fr resolutions 1,3 km L90
- perturbations from an AROME-Fr EDA (Y.michel):  
3D-var / 50 members / 3.2 km / 3h DA cycle
- DA 1h Cycle with 5 timeslots : 3\*15min + 2\*7min

4D-Var, 1-h Cycle

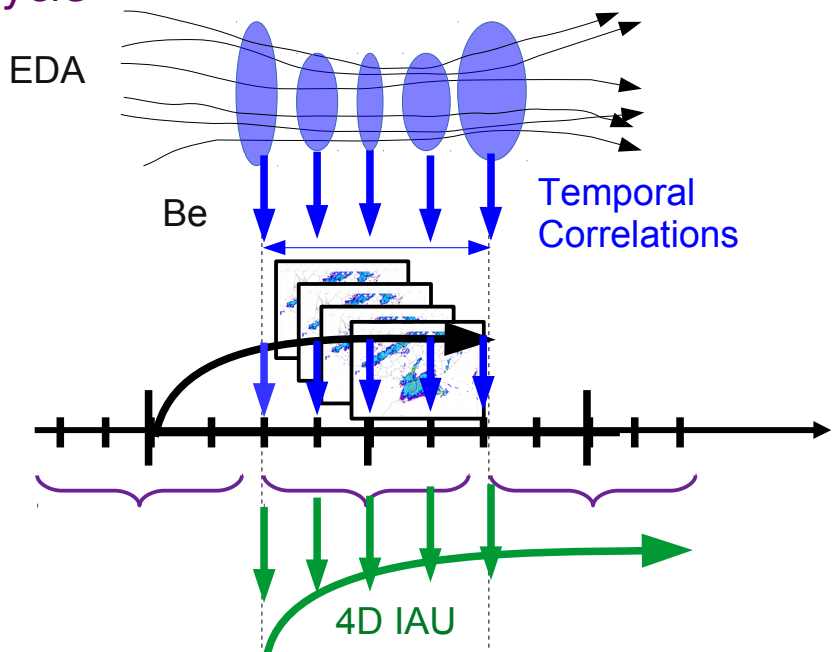


3D-Var, 1-h Cycle



1-h assimilation window

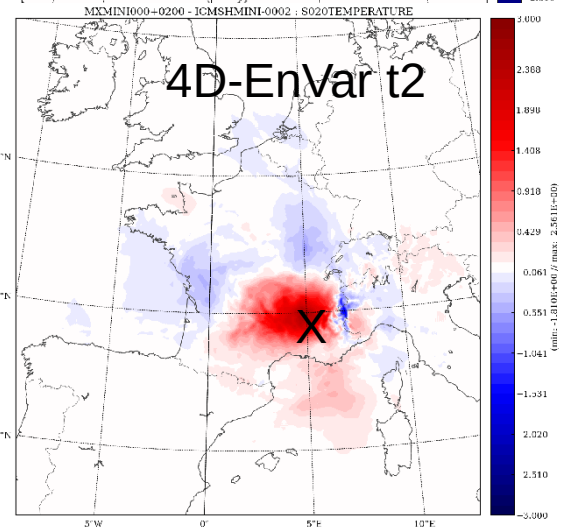
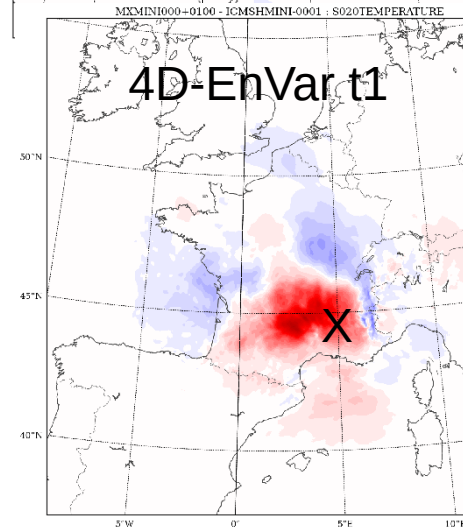
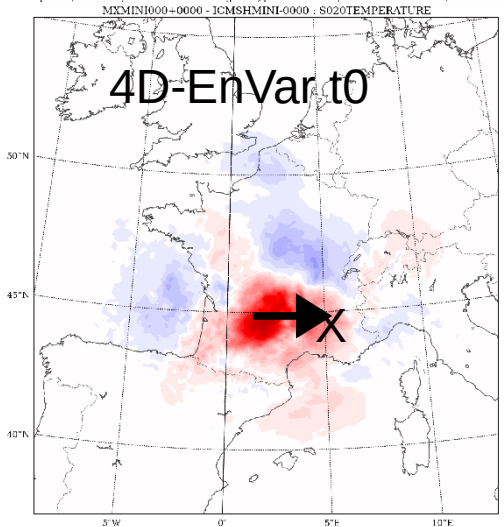
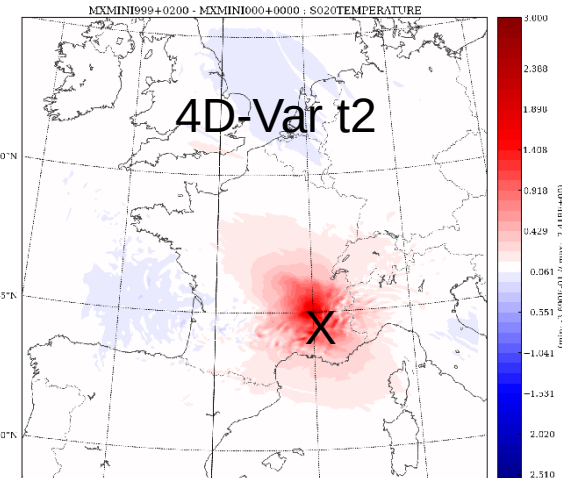
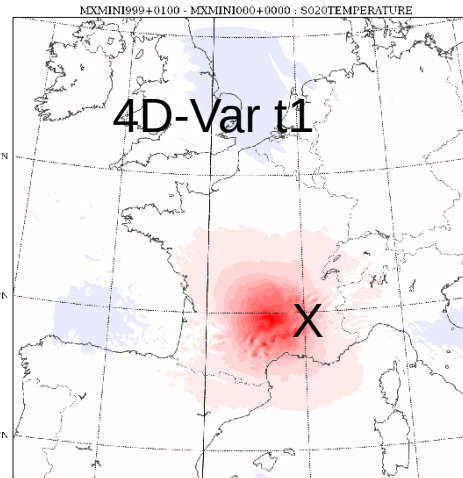
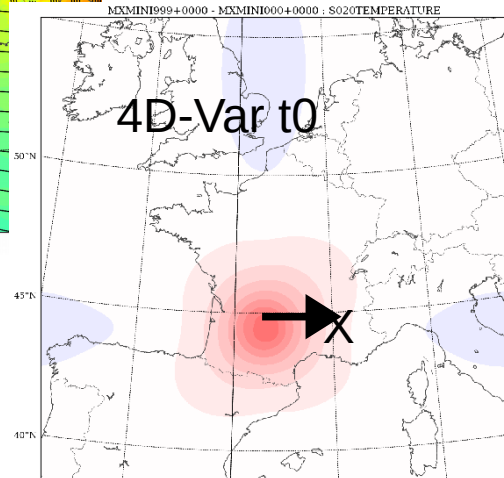
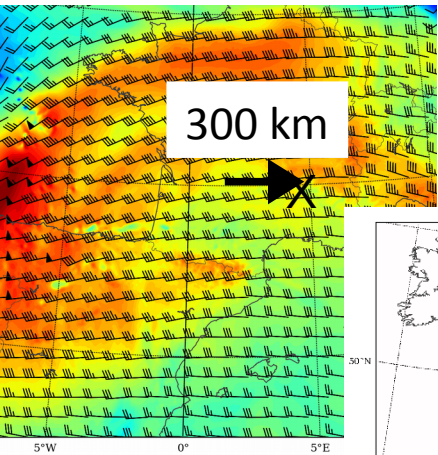
4DEnvar, 1-h Cycle



4D IAU

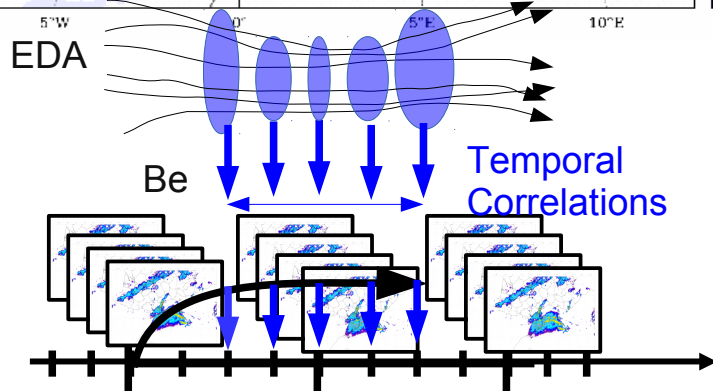
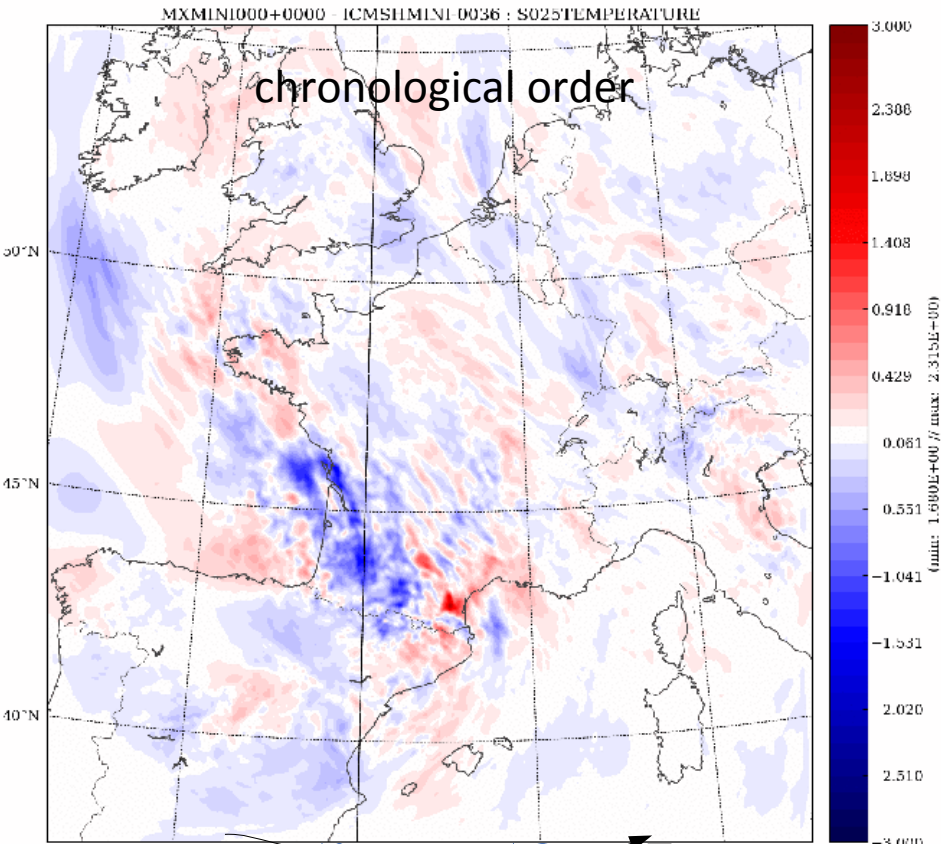
# 4D-EnVar: single obs in a 3h cycle : hourly increments

4° temperature innovation at 350 hPa at t+2h



# 4D Temperature increment

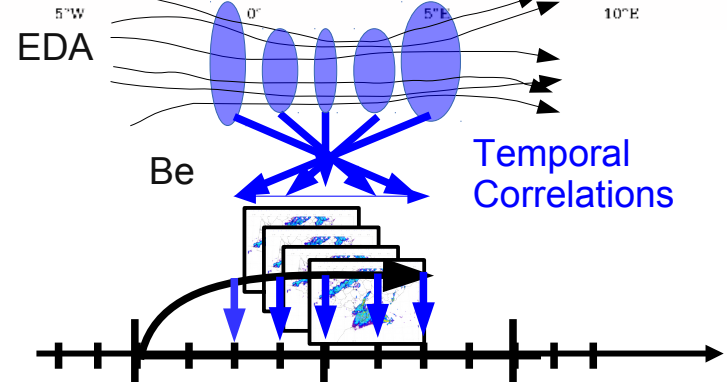
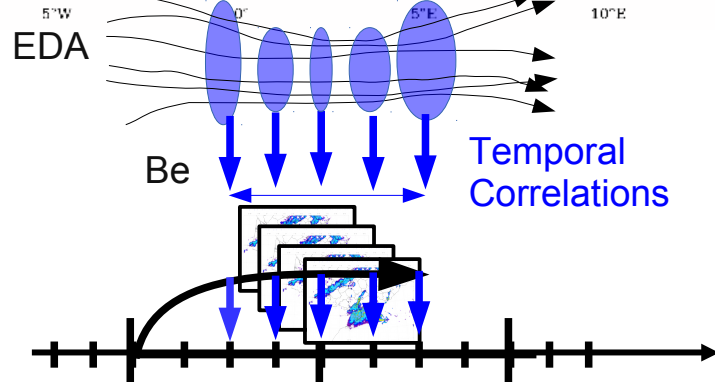
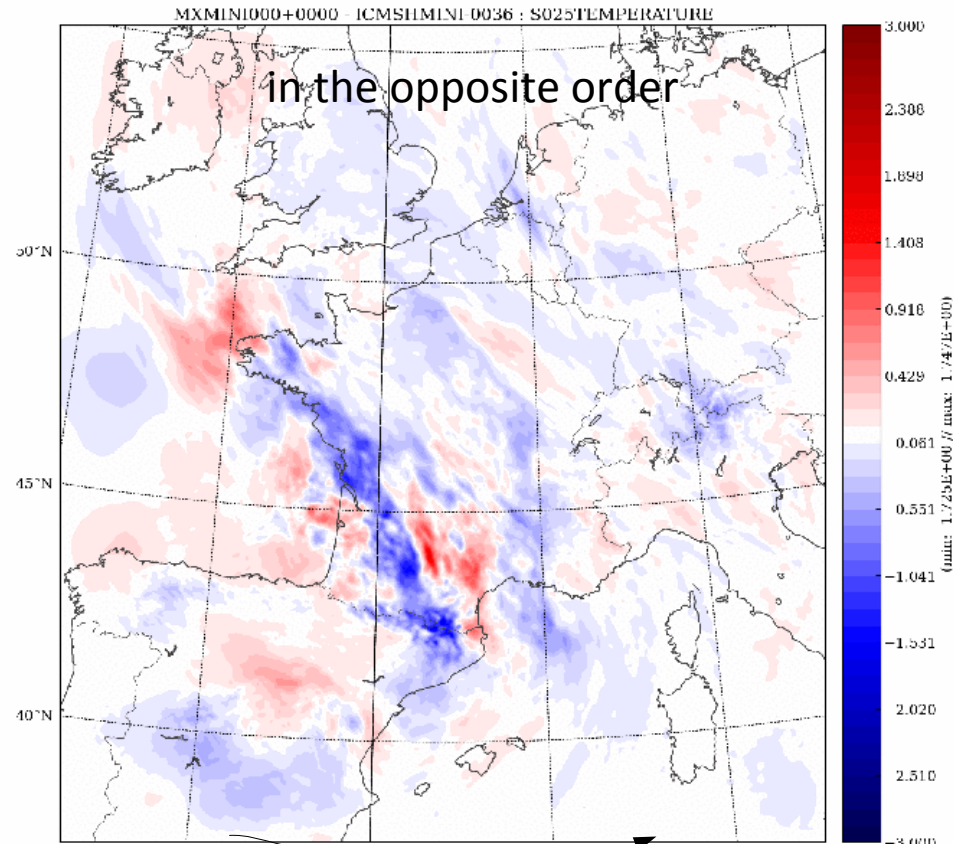
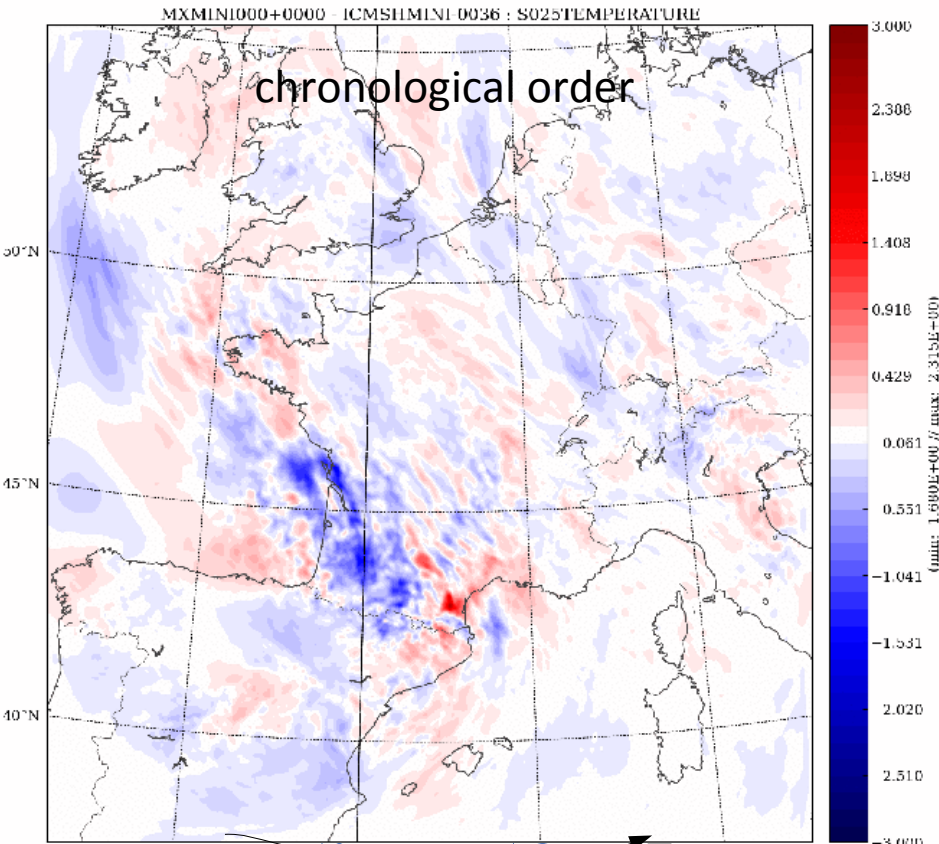
- temporal consistency





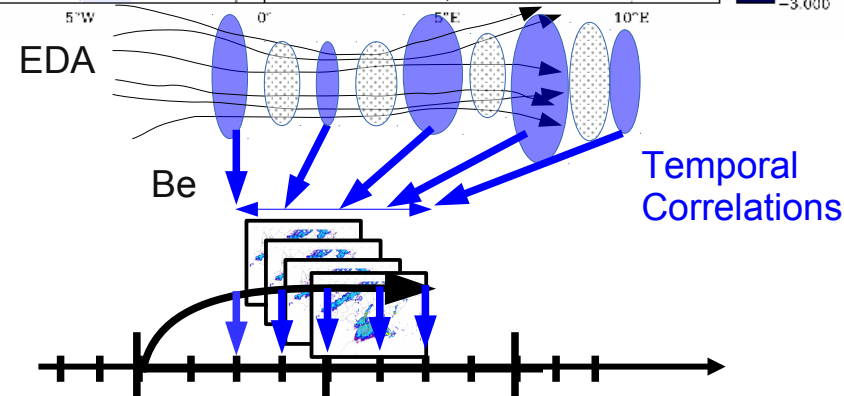
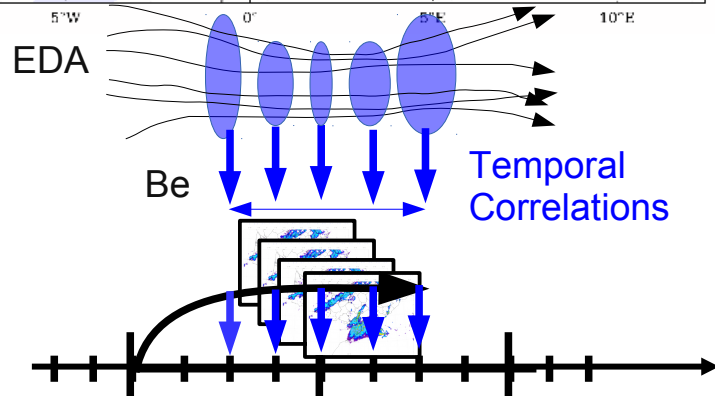
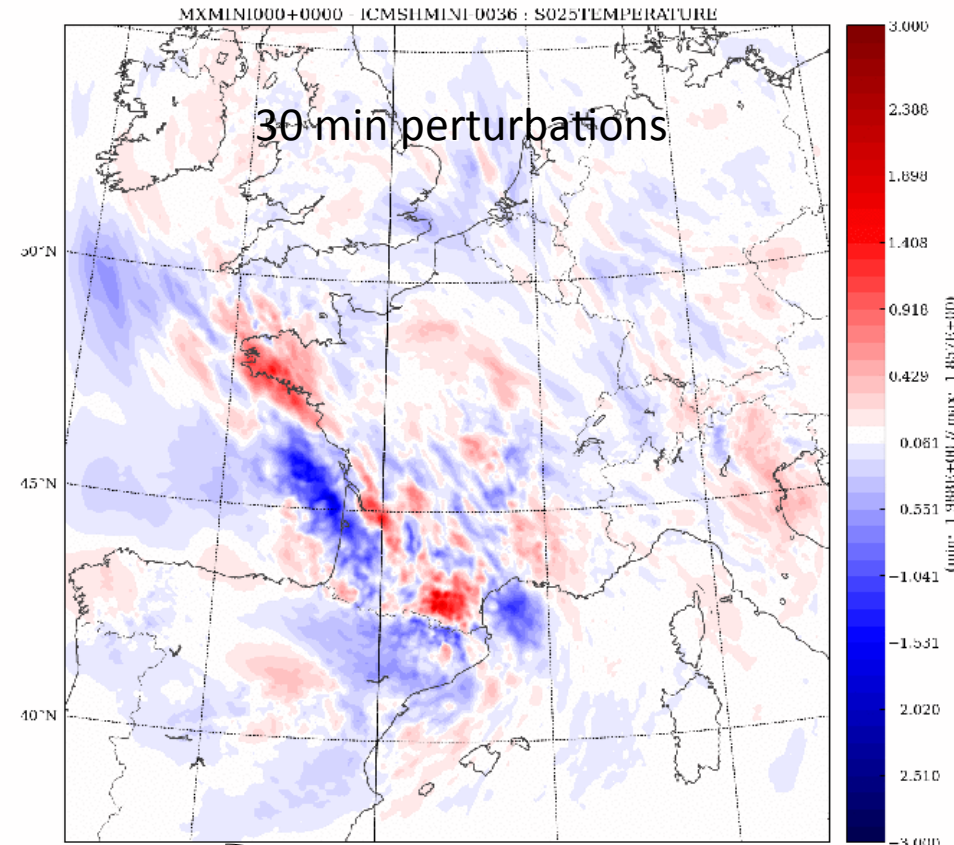
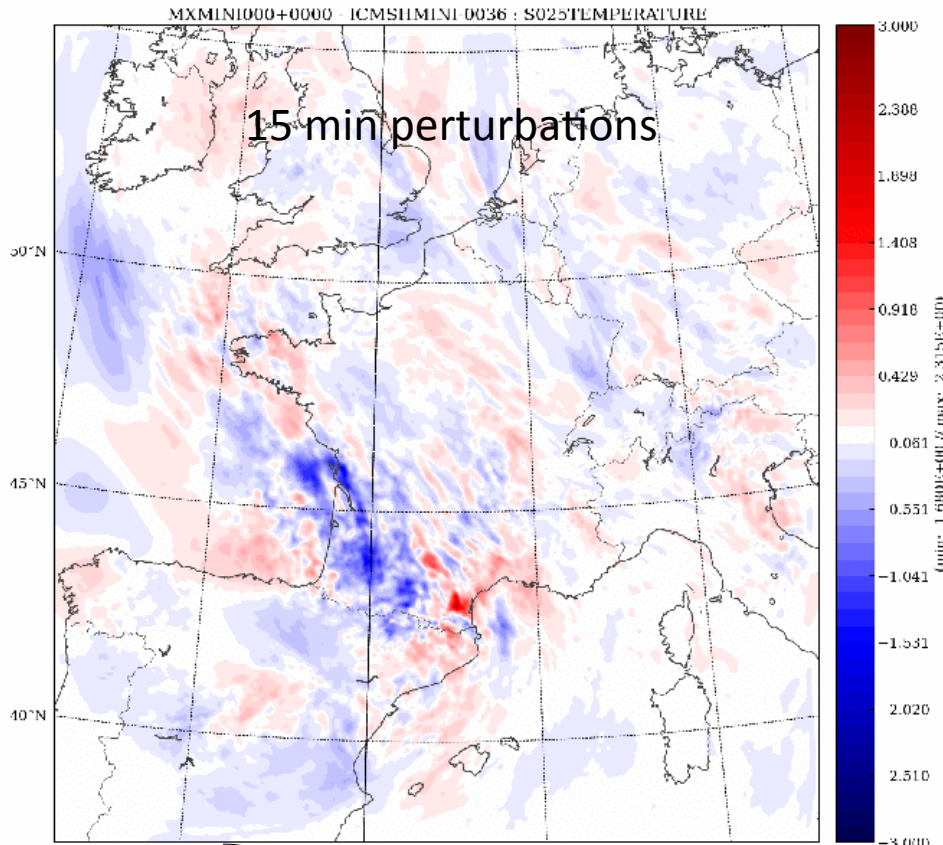
# 4D Temperature increment

- temporal consistency

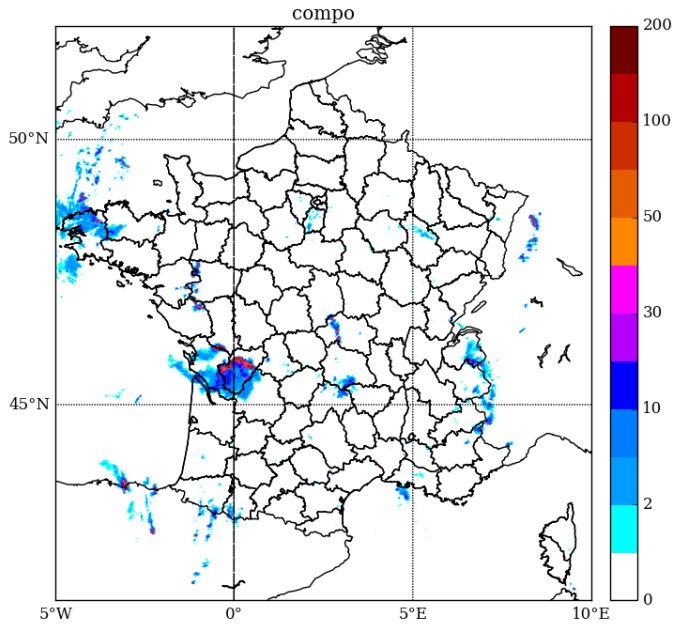


# 4D Temperature increment

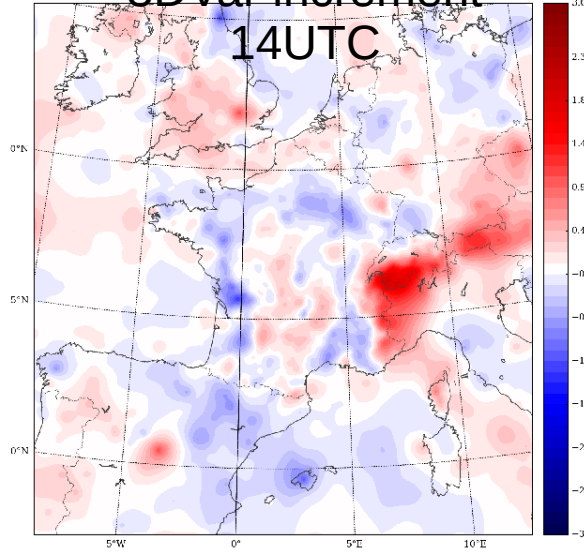
- temporal consistency



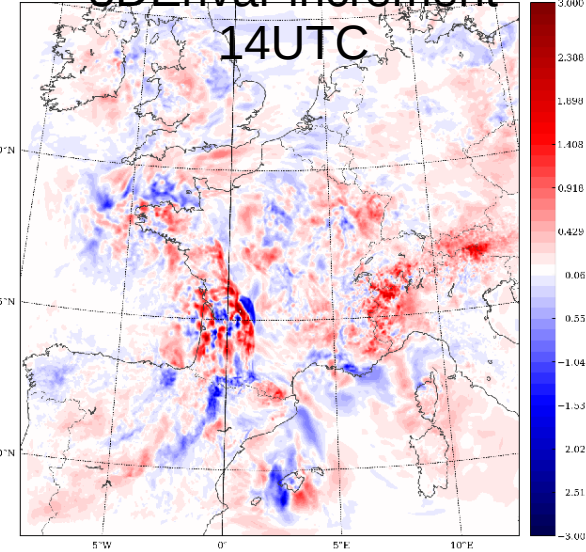
# 4DEnvar: 15 minutes increments



3DVar increment  
14UTC

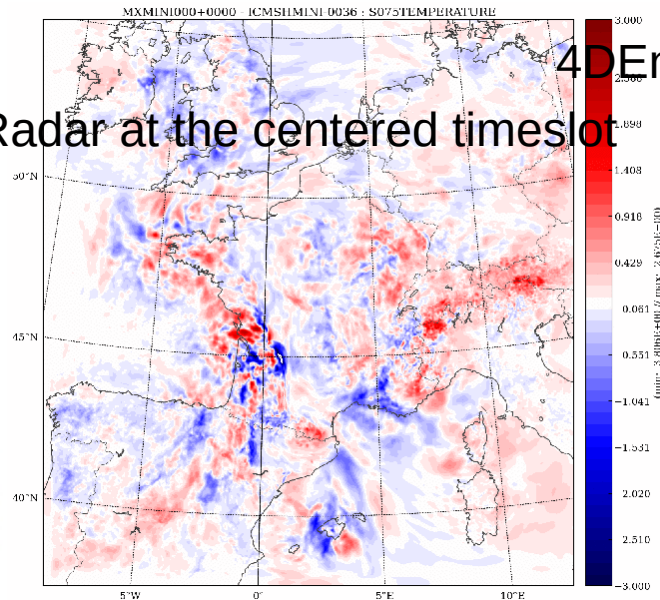


3DEnvar increment  
14UTC

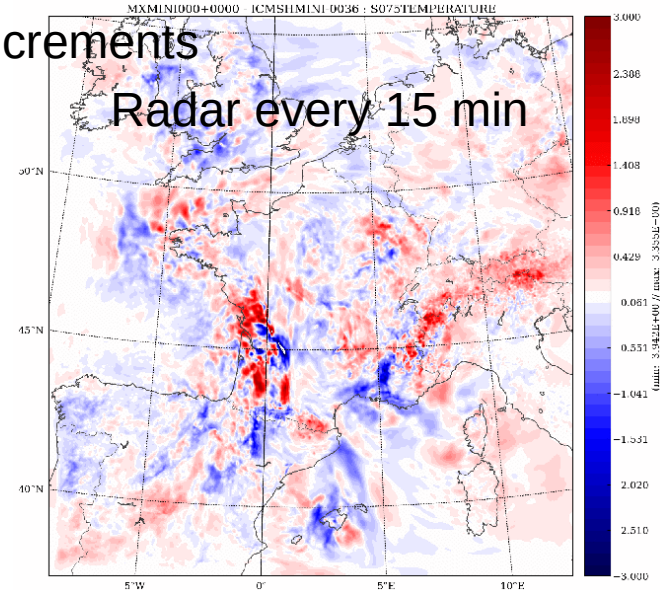


4DEnVar increments

Radar at the centered timeslot



Radar every 15 min

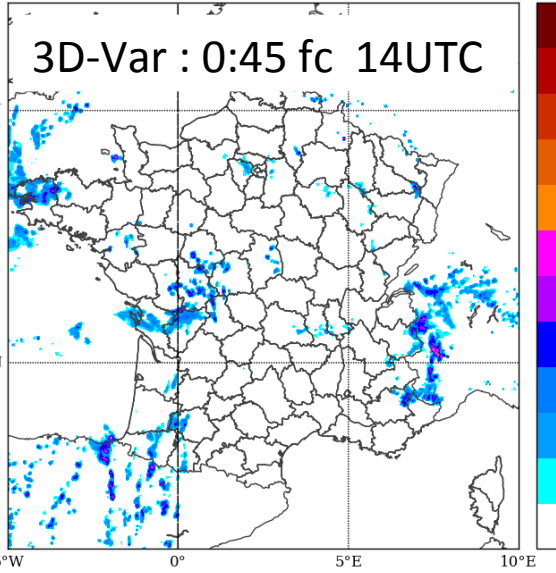


# 4DVar case study 26/05/2018

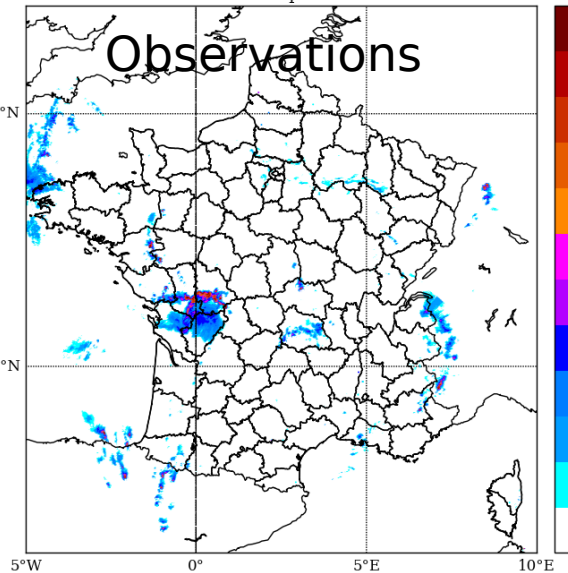
## Radar reflectivities at 14h45 UTC

3dvar

3D-Var : 0:45 fc 14UTC

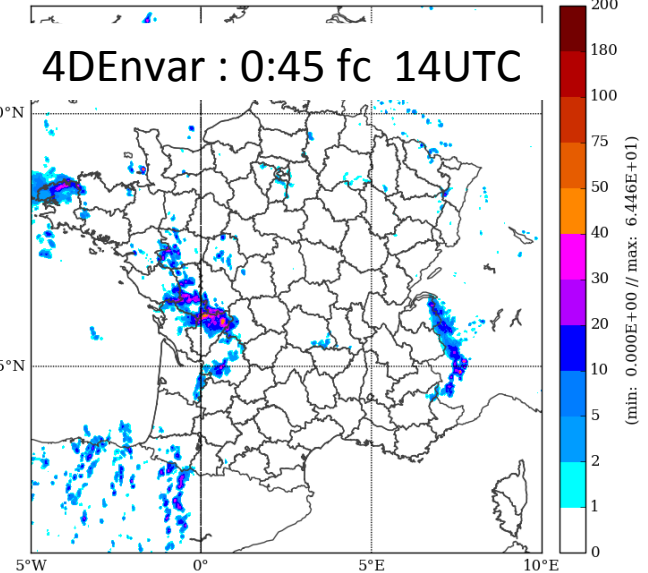


Observations



4denvar2

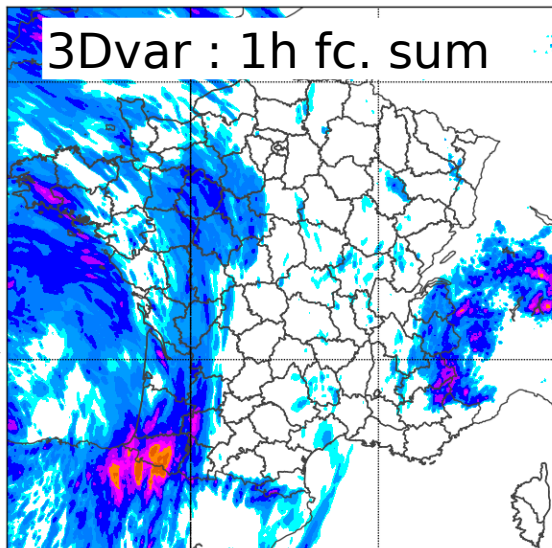
4DVar : 0:45 fc 14UTC



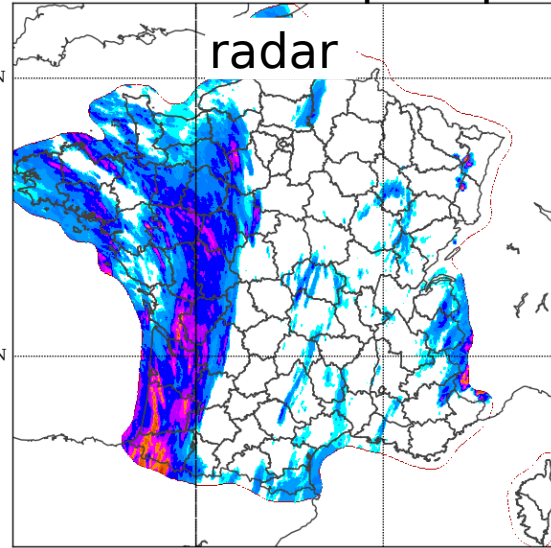
## 24 h cumulative precipitation

3dvar

3Dvar : 1h fc. sum

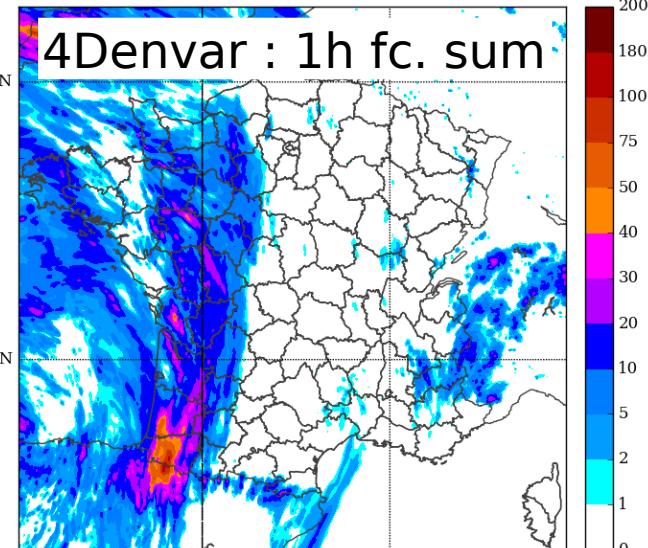


radar



4denvar iau sev15

4DVar : 1h fc. sum



# Conclusion : towards Envar systems at Météo-France

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## - towards Envar (3D and 4D ) scheme under OOPS :

### - Numerous ingredients already available and validated :

- B or B1/2 pre-conditioning
- control variable extending
- spectral/spatial localisation
- localisation length-scale dependent on the variable, height, scale
- advection of the localisation (4D)
- resolution changes
- variational bias correction (recent development)

### - Validation :

#### **3Denvar :**

- Encouraging results using a low resolution configuration
- To be confirmed with the full system over a long period

#### **4Denvar :**

- Encouraging results on case studies
- Validation over a long period to be done (new HPC)

**In operations in 2022 ?**

# References

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Montmerle, T., Michel, Y., Arbogast, E., Ménétrier, B., & Brousseau, P. (2018). A 3D ensemble variational data assimilation scheme for the limited-area AROME model: Formulation and preliminary results. *Quarterly Journal of the Royal Meteorological Society*, 144(716), 2196-2215.