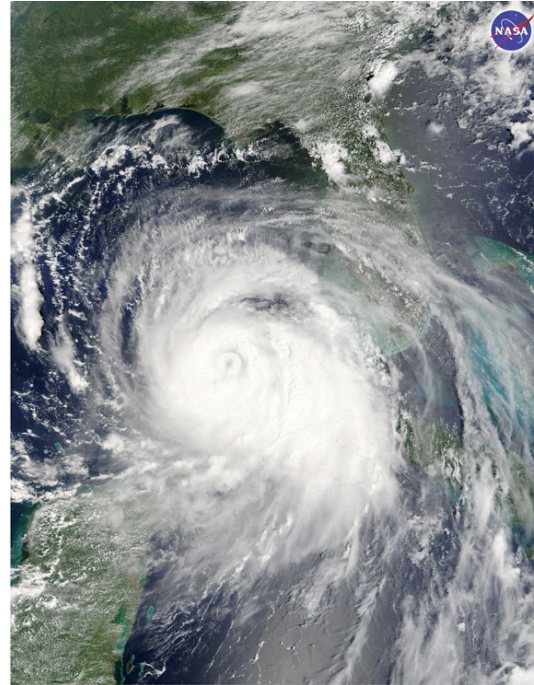
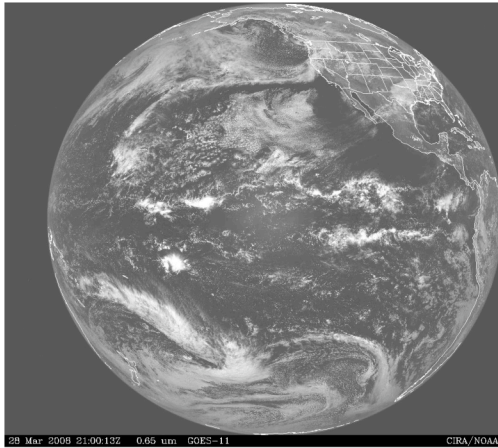
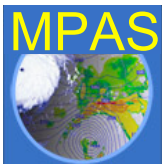


# Model for Prediction Across Scales (MPAS)



Joe Klemp, Bill Skamarock (NCAR)  
Todd Ringler (Los Alamos National Laboratory)  
John Thuburn (University of Exeter, UK)

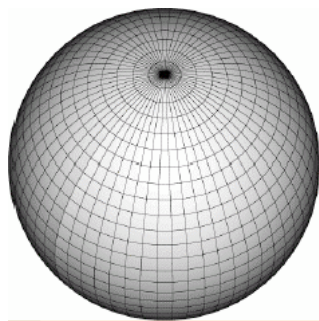


# Future Weather/Climate Atmospheric Dynamic Core

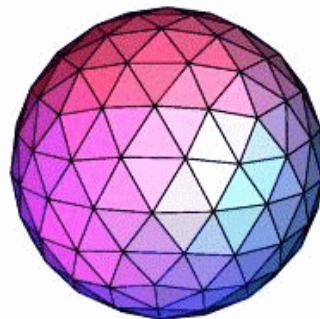
## Problems with lat-lon coordinate for global models

- Pole singularities require special filtering
- Polar filters do not scale well on massively parallel computers
- Highly anisotropic grid cells at high latitudes

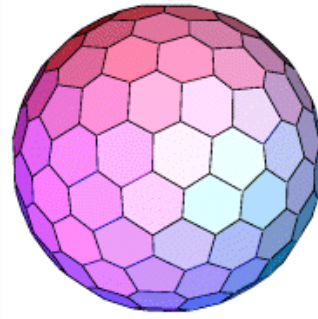
Consideration of alternative spatial discretizations:



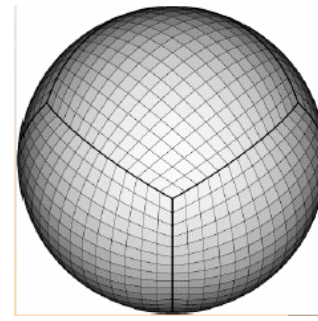
Lat-Lon



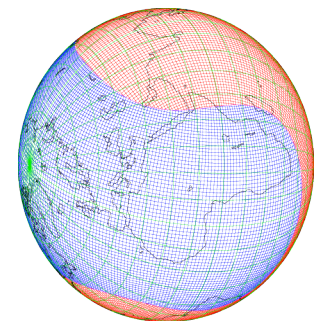
Icosahedral-triangles



Icosahedral-hexagons

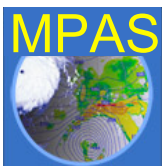


Cubed Sphere



Yin-Yang

- Priority Requirements:**
- Efficient and scales well on massively parallel computers
  - Well suited for cloud (nonhydrostatic) to global scales
  - Capability for local grid refinement and regional domains
  - Conserves at least mass and scalar quantities



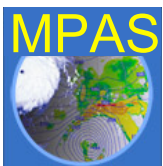
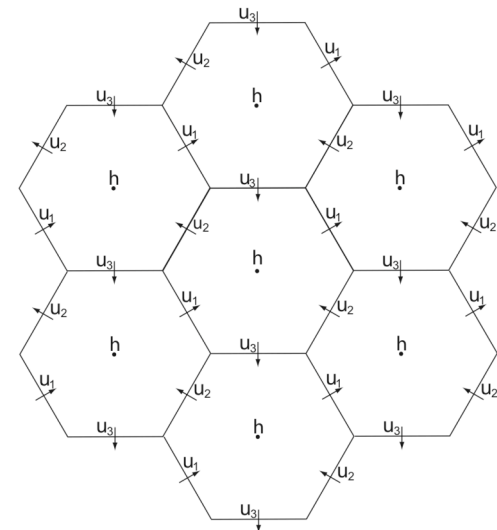
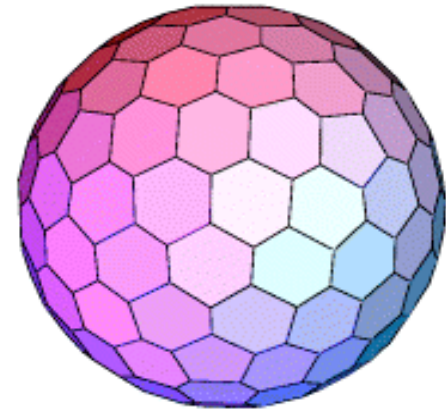
# Hexagonal C-Grid

## Why a hexagonal grid?

- Removes the pole singularity
- Most isotropic (wave propagation).
- Provides good conservation properties in a finite-volume formulation
- Hexagonal grid permits larger explicit time steps.
- Readily generalized to arbitrarily structured grids

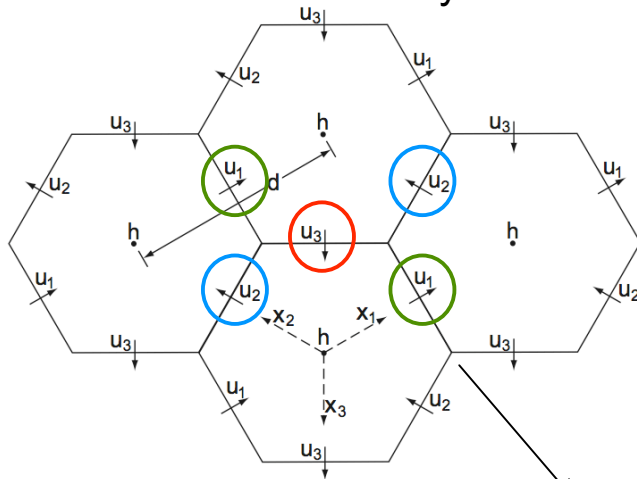
## Why a C-grid staggering?

- Provides the highest accuracy for the fast (gravity-wave) modes
- Provides twice the resolution of the A grid, and avoids the parasitic mode

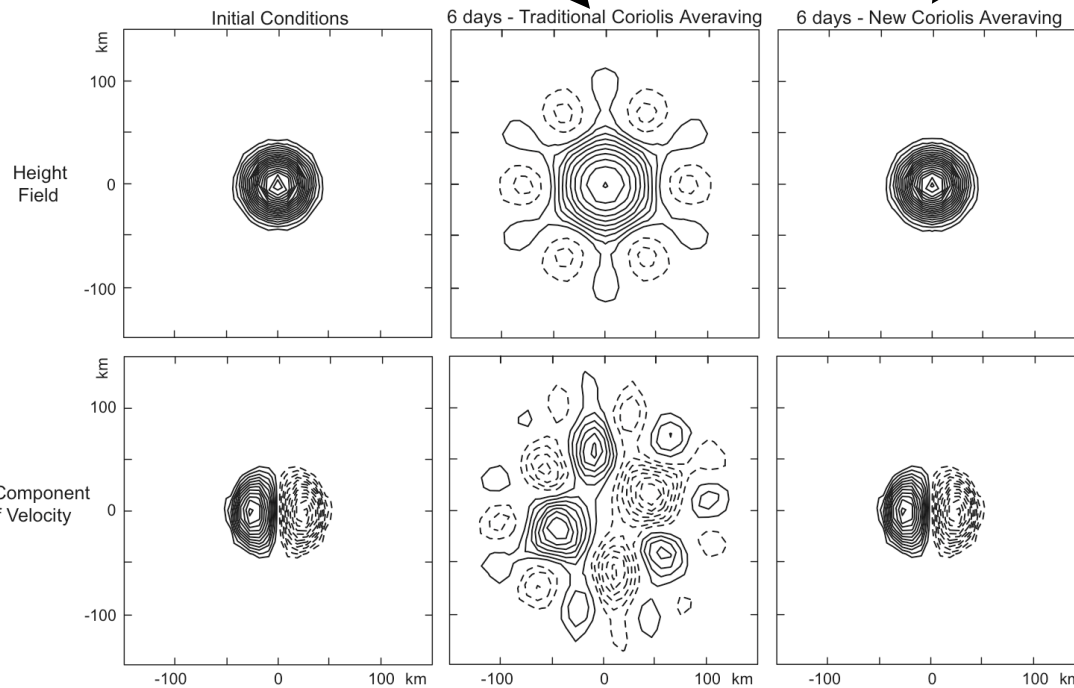
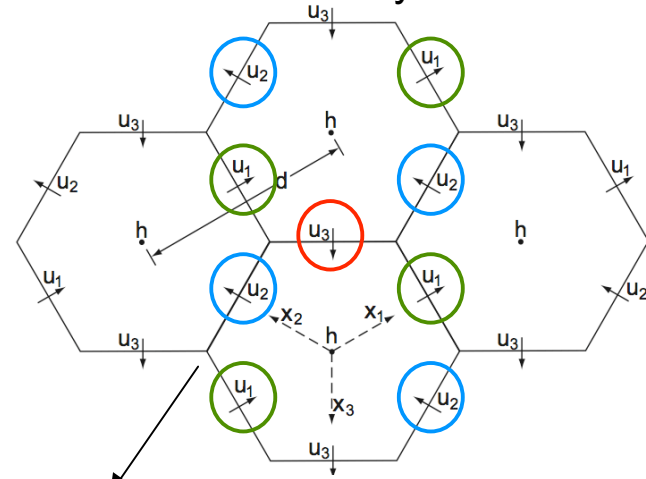


# Hexagonal C-Grid Problem: Non-Stationary Geostrophic Mode

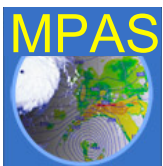
Traditional Coriolis velocity construction



New Coriolis velocity construction

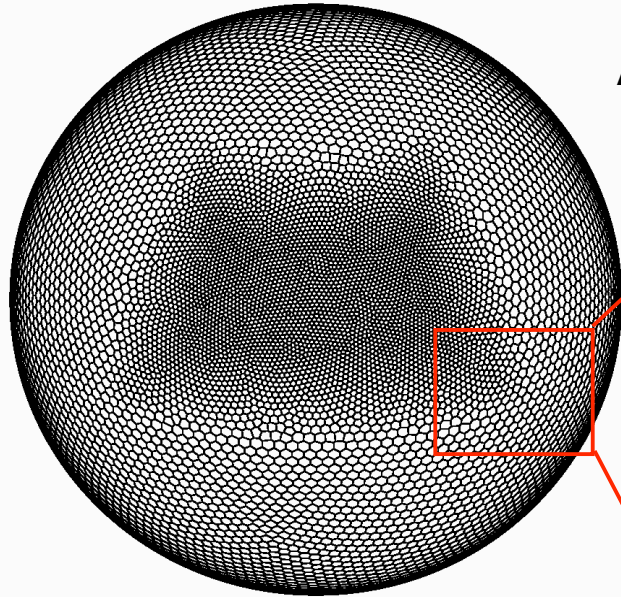


Stationary geostrophic mode is recovered!

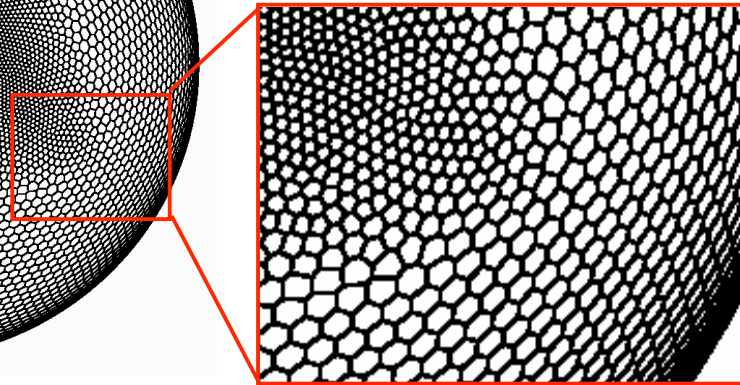




# Conformal, Variable-Resolution Meshes



A conformal mesh is a mesh with no hanging nodes.



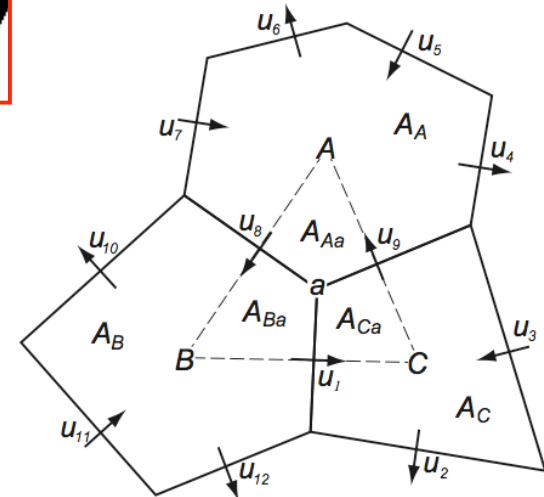
Cell center is cell center-of-mass

Edges of dual grid intersect edges of primary grid at right angles.

*Conjecture:* smooth refinement on conformal meshes should mitigate many refinement problems.

## SCVTs Spherical Centroidal Voronoi Tessellations

(Includes Lat/Lon and conformally-mapped cubed sphere.)



(Michael Duda, MMM)

# Generalization for Arbitrarily Structured Grids

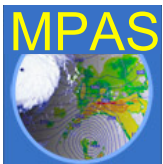
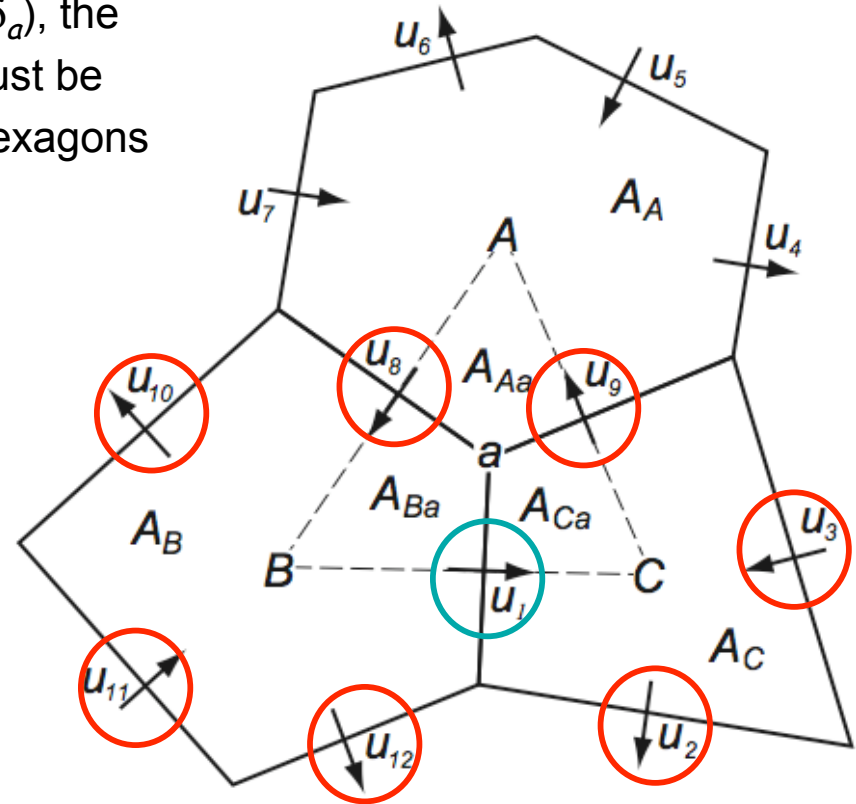
In discrete analogue of vorticity equation ( $\xi_t = -f\delta_a$ ), the divergence  $\delta_a$  on the Delaunay triangulation must be identical to the divergence  $\delta_A$  on the Voronoi hexagons used in the height equation ( $h_t = -H\delta_A$ ):

$$A_a \delta_a = A_{Aa} \delta_A + A_{Ba} \delta_B + A_{Ca} \delta_C$$

Construct tangential velocities from weighted sum of normal velocities on edges of adjacent grid cells.

$$d_e u_e^\perp = \sum_j w_e^j l_j u_j$$

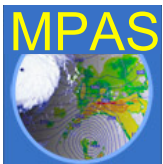
Energy conservation achieved by requiring  $w_e^j = -w_j^e$ .



# Analytic Results for the Nonlinear Shallow-Water Equations

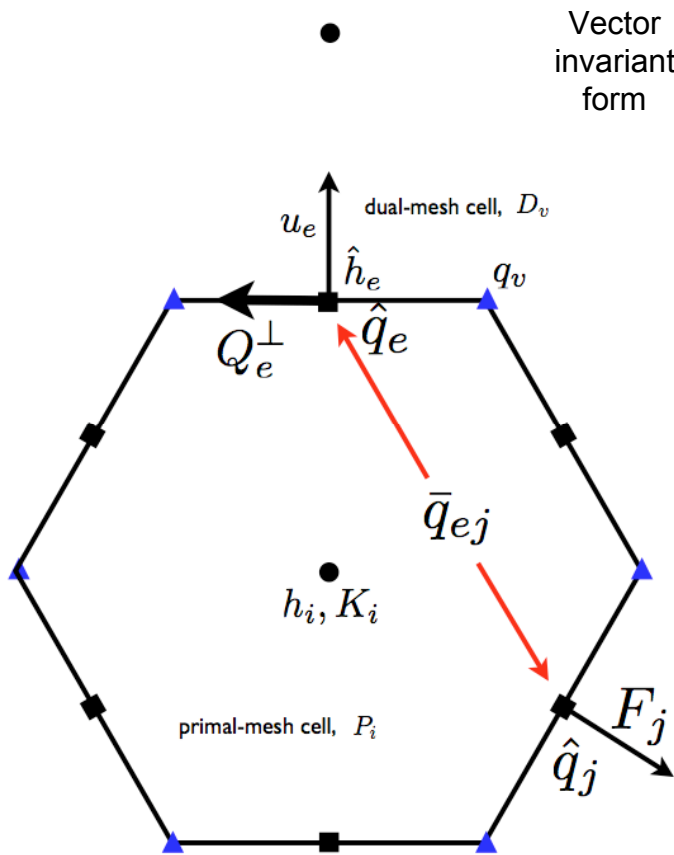
1. Stationary geostrophic mode is recovered.
2. Potential vorticity is conserved to round-off. PV is compatible with an underlying thickness evolution equation.
3. Total energy is conserved to within time truncation.
  - a. Coriolis force is energetically-neutral
  - b. Transport of KE is conservative
  - c. KE/PE exchange is equal and opposite.
4. It appears that potential enstrophy can be dissipated.

*Results hold for a wide class of meshes:* Lat/Lon, Voronoi Tessellations, Delaunay Triangulation and Conformally-mapped cubed sphere meshes.



# Reconstructing the Nonlinear Coriolis Force

(The nonlinear Coriolis force  $Q_e^\perp$  is the PV flux perpendicular to the velocity)



$$\frac{\partial u_e}{\partial t} + \hat{q}_e [hu]_e^\perp = [\nabla (gh_i + K_i)]_e$$

$$\frac{\partial u_e}{\partial t} + Q_e^\perp = [\nabla (gh_i + K_i)]_e$$

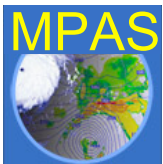
$$d_e Q_e^\perp = \sum_j w_e^j l_j F_j \bar{q}_{ej}$$

$$F_j = \hat{h}_j u_j \quad \text{thickness flux}$$

$$w_e^j = -w_j^e \quad \text{weights are equal and opposite}$$

$$\bar{q}_{ej} = \bar{q}_{je} \quad \text{PV is symmetric}$$

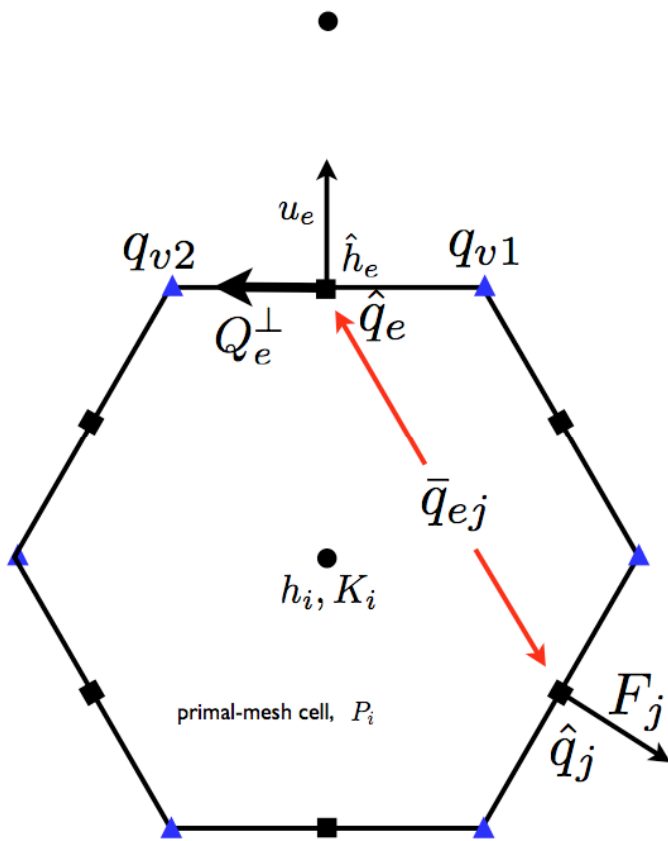
The nonlinear Coriolis force will be energy neutral for any  $\bar{q}_{ej}$





# Reconstructing the Nonlinear Coriolis Force

(The nonlinear Coriolis force  $Q_e^\perp$  is the PV flux perpendicular to the velocity)



$$\frac{\partial u_e}{\partial t} + \hat{q}_e [hu]_e^\perp = [\nabla (gh_i + K_i)]_e$$

$$\frac{\partial u_e}{\partial t} + Q_e^\perp = [\nabla (gh_i + K_i)]_e$$

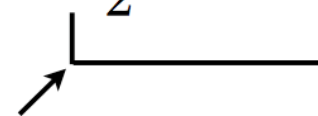
Energy conservation is obtained by:

$$\bar{q}_{ej} = \bar{q}_{je} = \frac{1}{2} (\hat{q}_e + \hat{q}_j)$$

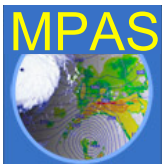
Energy is conserved for any  $\hat{q}_e$  and any  $\hat{q}_j$ !

The APVM is obtained by:

$$\hat{q}_e = \frac{1}{2} (q_{v1} + q_{v2}) - \frac{dt}{2} \mathbf{u} \cdot \nabla q$$

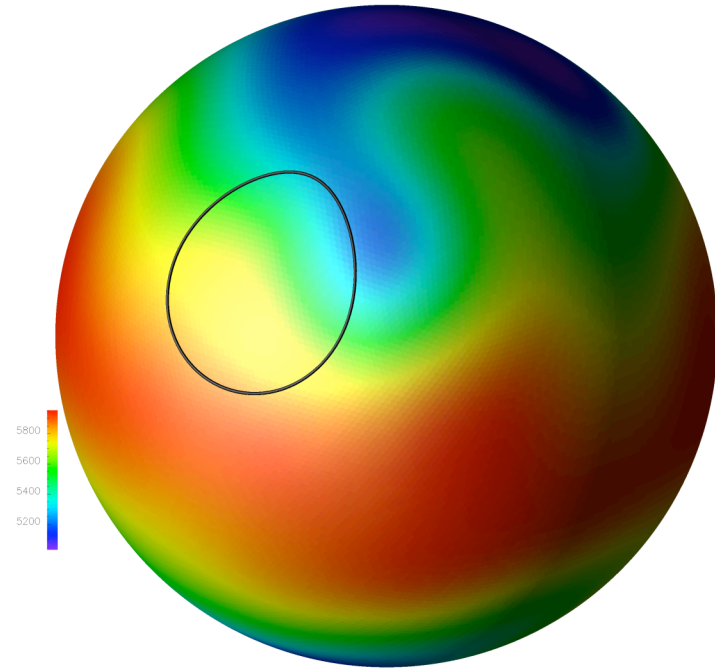
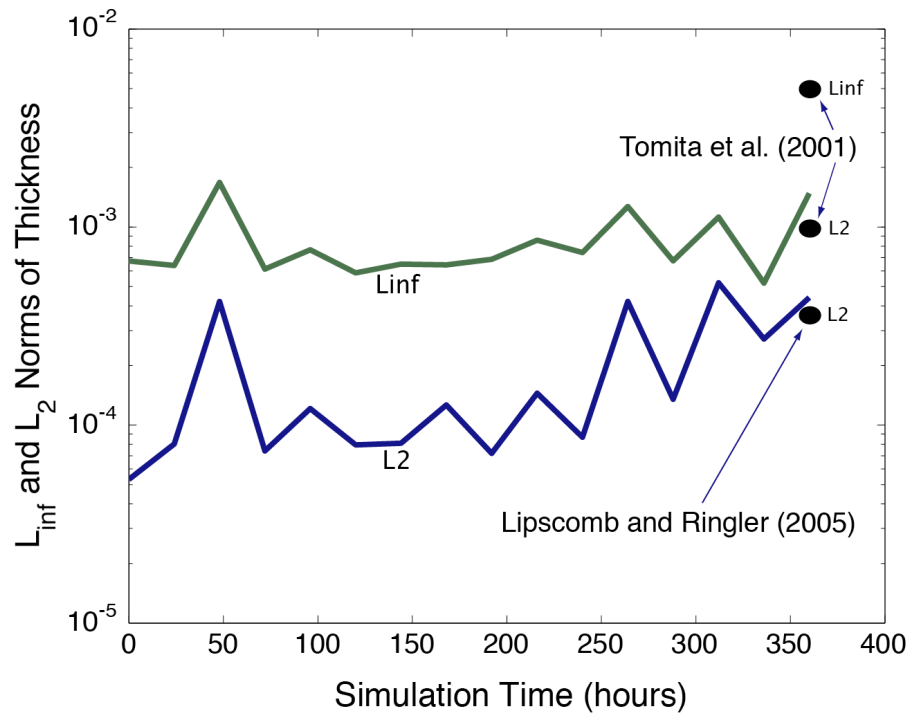


Upstream bias leads to dissipation of potential enstrophy.

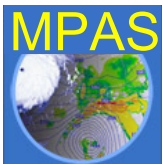


# Shallow-Water Test Case 5: Flow over an Isolated Mountain

40962 cells,  $dx \sim 120$  km  
2nd order differencing  
RK4 time differencing

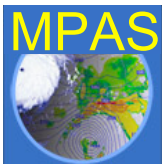
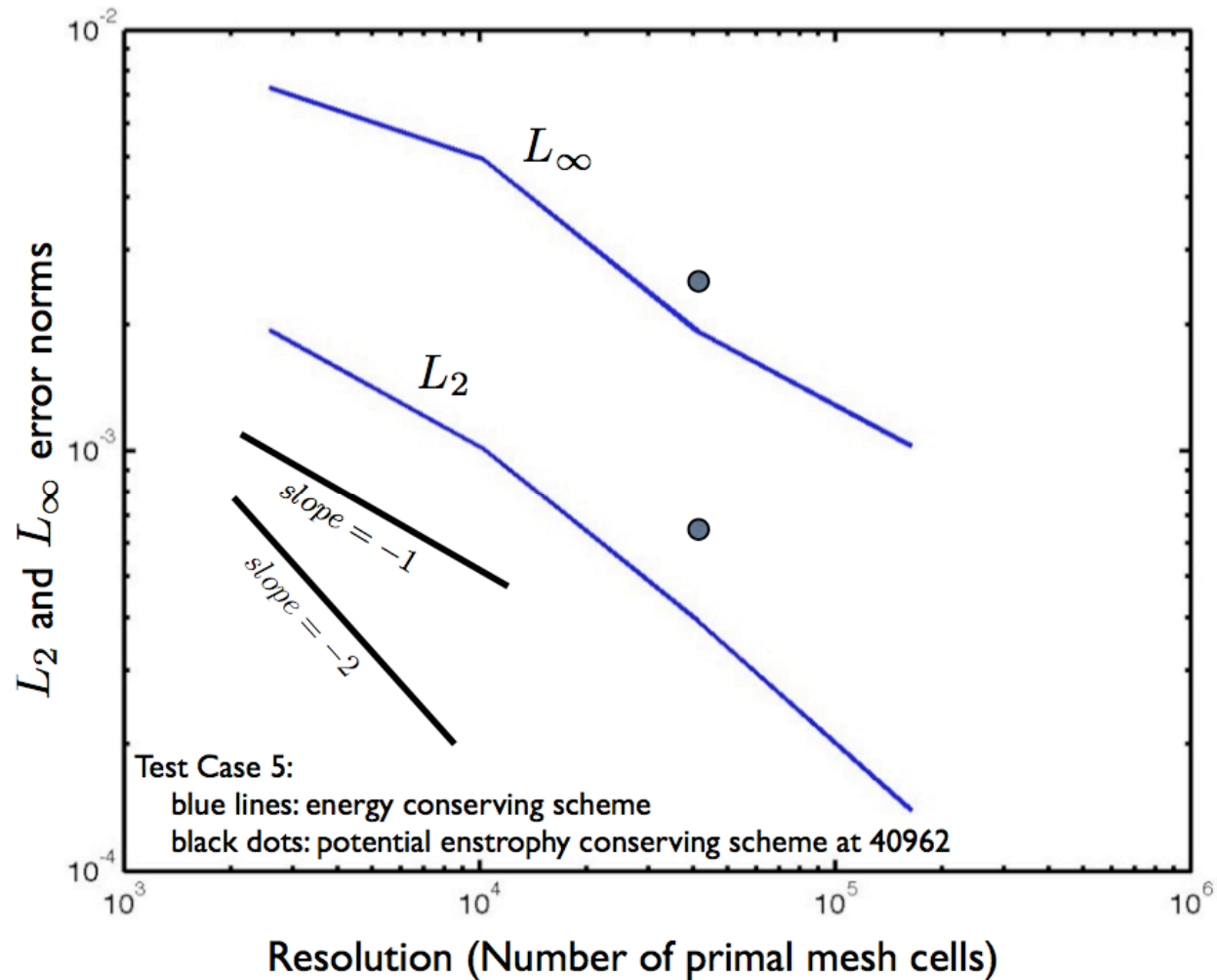


*Results with quasi-uniform meshes:*  
New scheme is competitive  
with existing models.



(Todd Ringler, LANL)

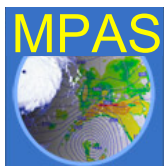
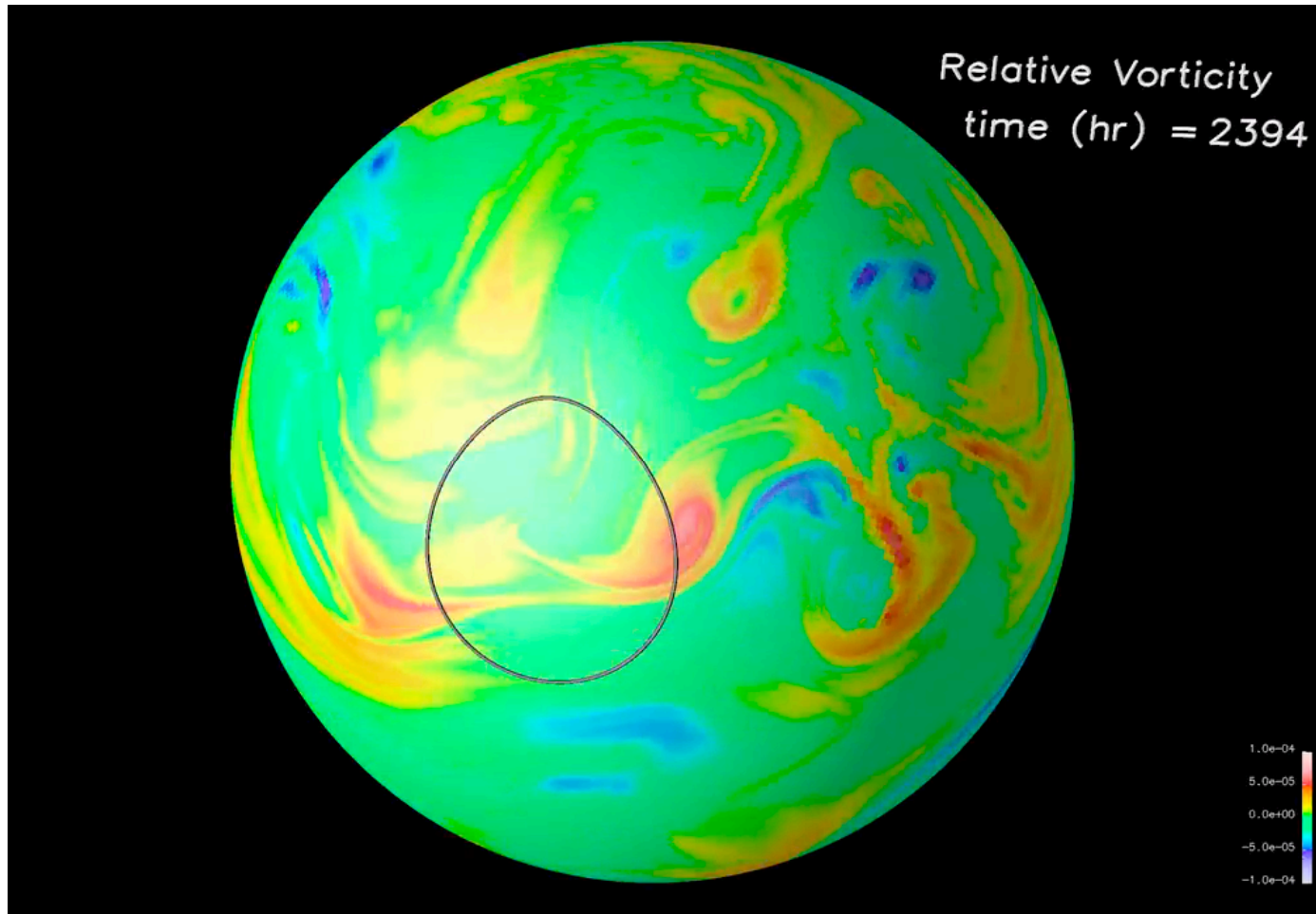
# SWTC#5: Convergence Rate as Measured by $L_2$ and $L_\infty$ Norms



# SWTC#5: 100 Day Integration, Variable-Res Mesh

Computing potential vorticity with an upstream bias allows potential enstrophy dissipation while conserving energy

$d \sim 40$  km over terrain  
 $\sim 120$  km elsewhere

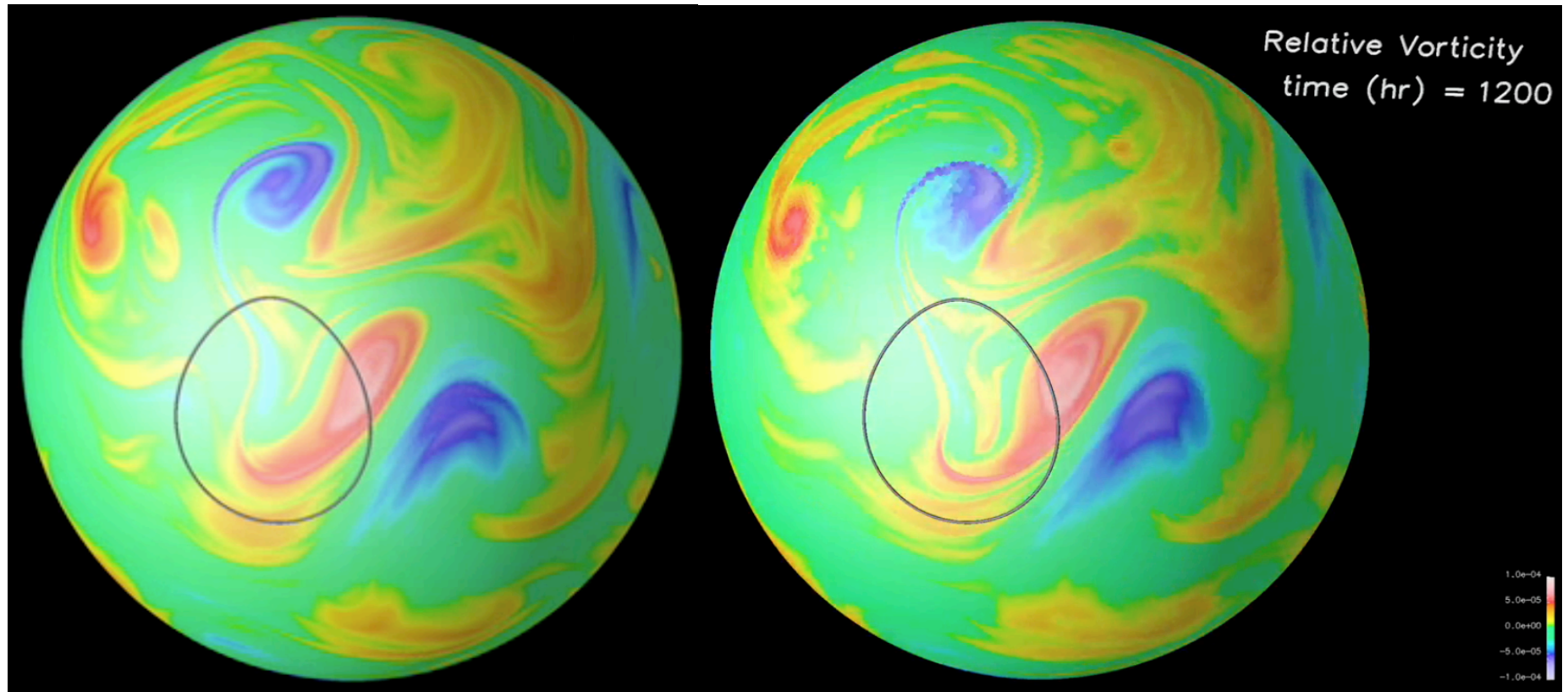


(Todd Ringler, LANL)



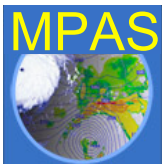
# SWTC#5 Relative Vorticity at 50 Days: Impact of Variable Mesh

Energy conserving and potential enstrophy dissipating simulation



Constant mesh,  $d \sim 60$  km

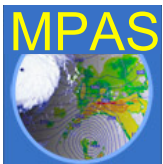
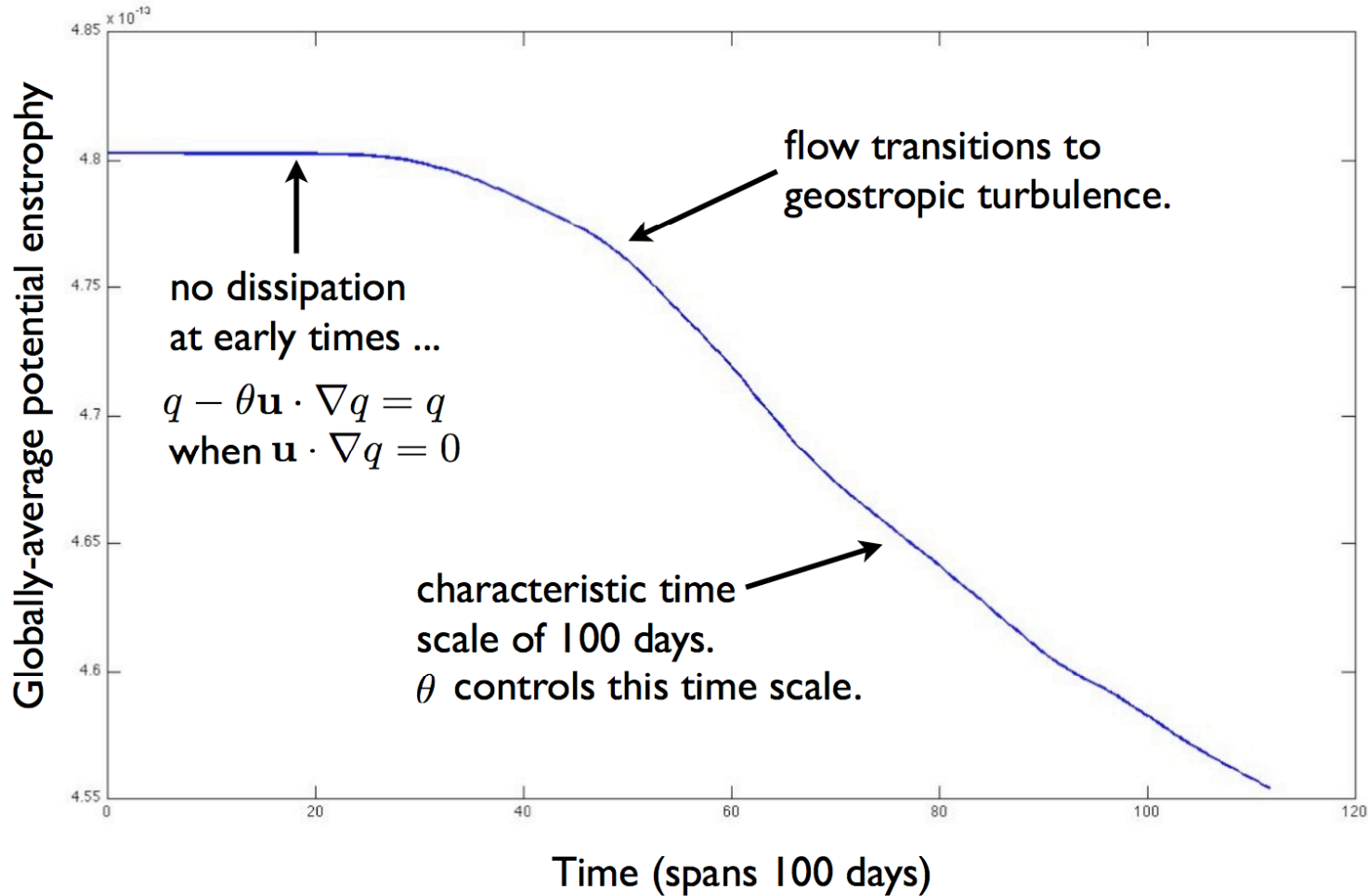
Variable Mesh,  $d \sim 40 - 120$  km



(Todd Ringler, LANL)

# SWTC#5: Globally-Averaged Potential Enstrophy Evolution

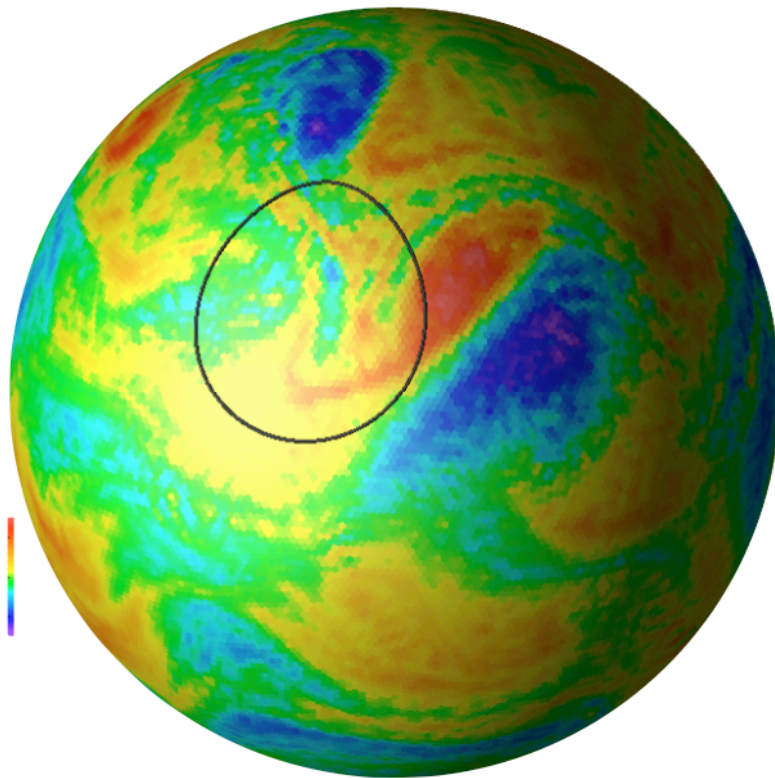
Using upstream bias for potential vorticity interpolation



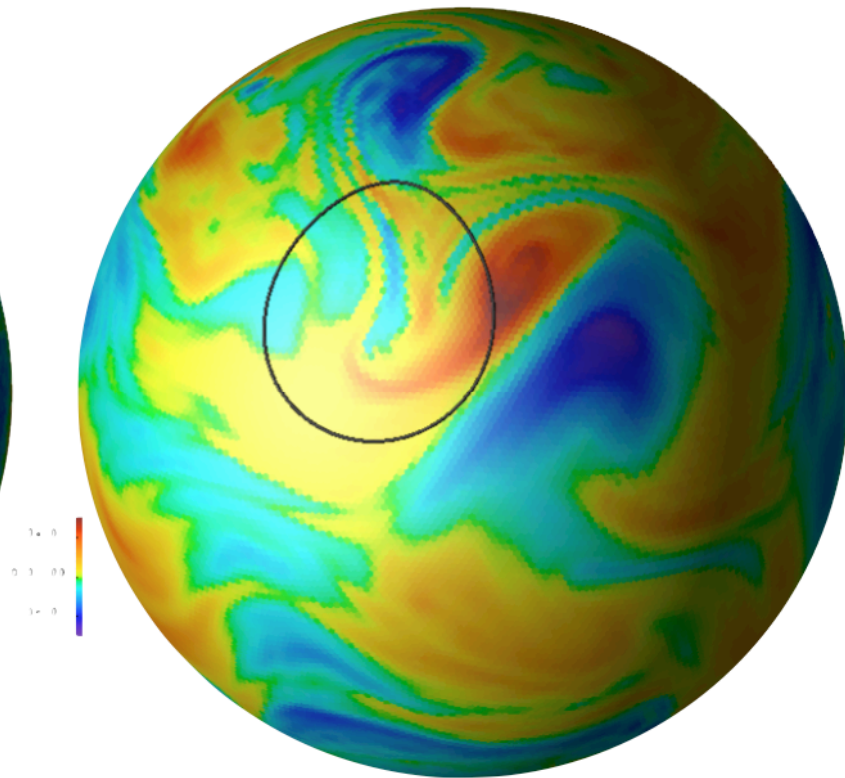
(Todd Ringler, LANL)

## SWTC#5 Relative Vorticity at 50 days: Impact of Dissipating Potential Enstrophy

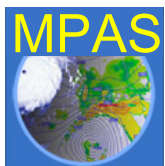
Enstrophy conserving - PV flux  
Computed without upstream bias



Enstrophy dissipating - PV flux  
Computed with upstream bias

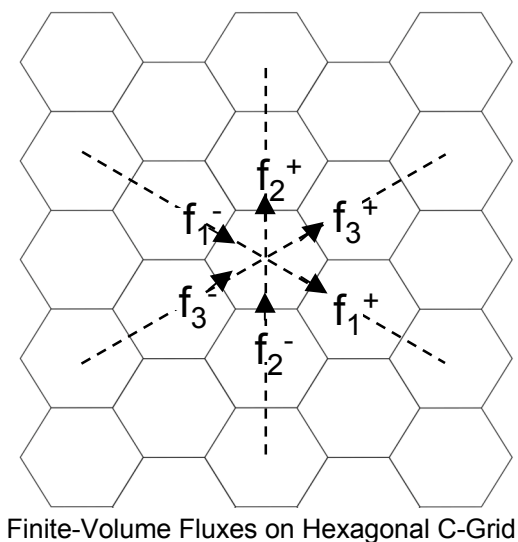


Both simulations conserve energy to  $1e^{-8}$



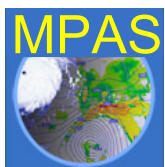
(Todd Ringler, LANL)

# Limited-Area Cloud Model on Hexagonal C-Grid

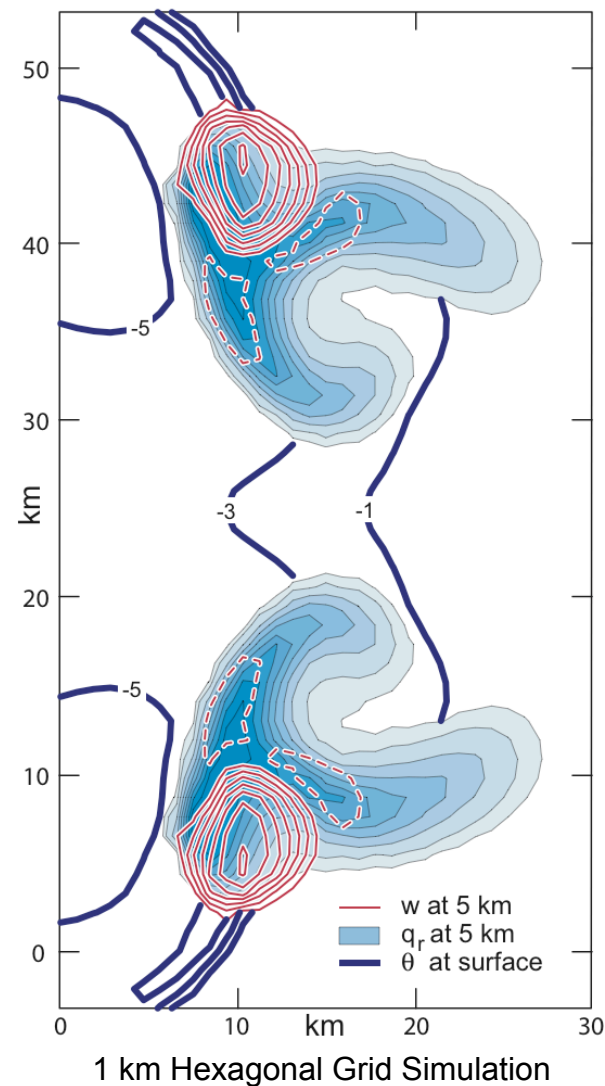


## Research Progress:

- Constructed a 3-D limited-area hexagonal-grid cloud model based on WRF/ARW numerics to evaluate performance.
- Documented that hexagonal-grid cloud simulations are at least as accurate and computationally more efficient than those on a conventional rectangular grid.



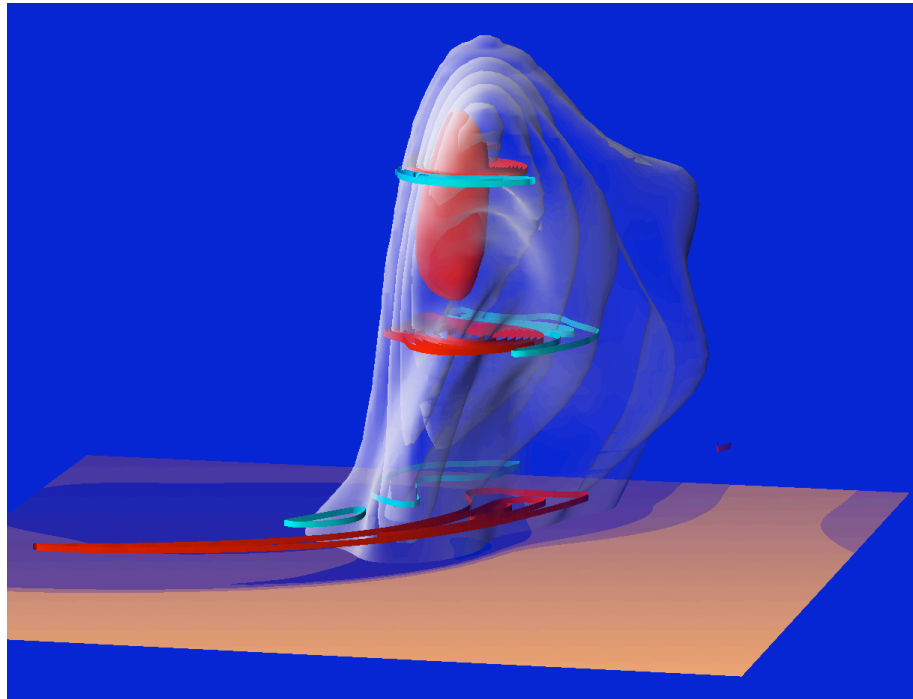
Splitting Supercell at 2 hours



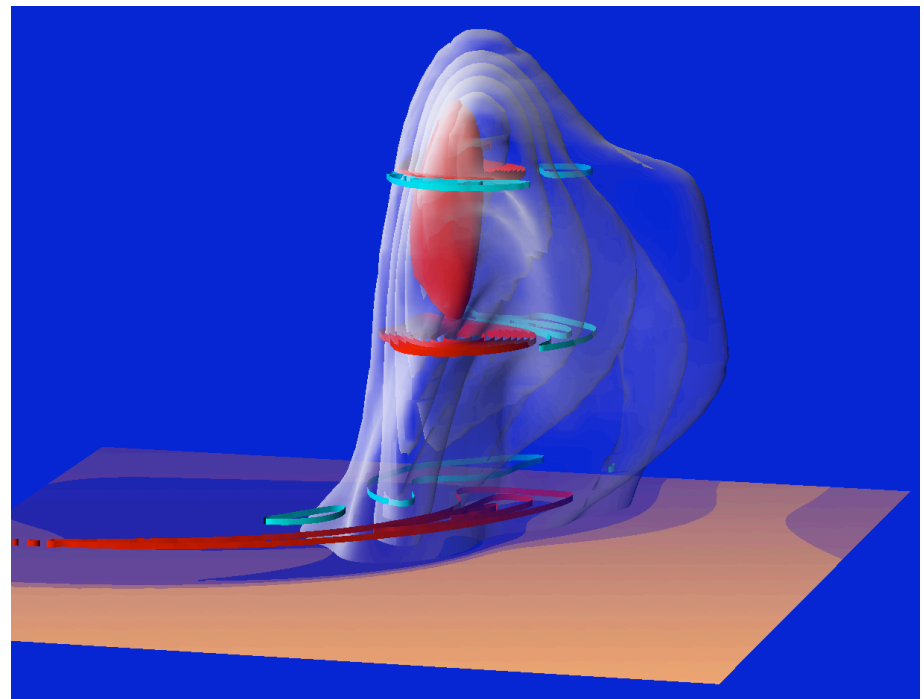


# 3-D Supercell Simulation ~500 m Horizontal Grid

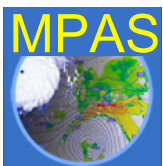
Rectangular Grid



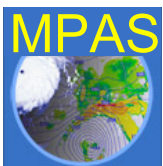
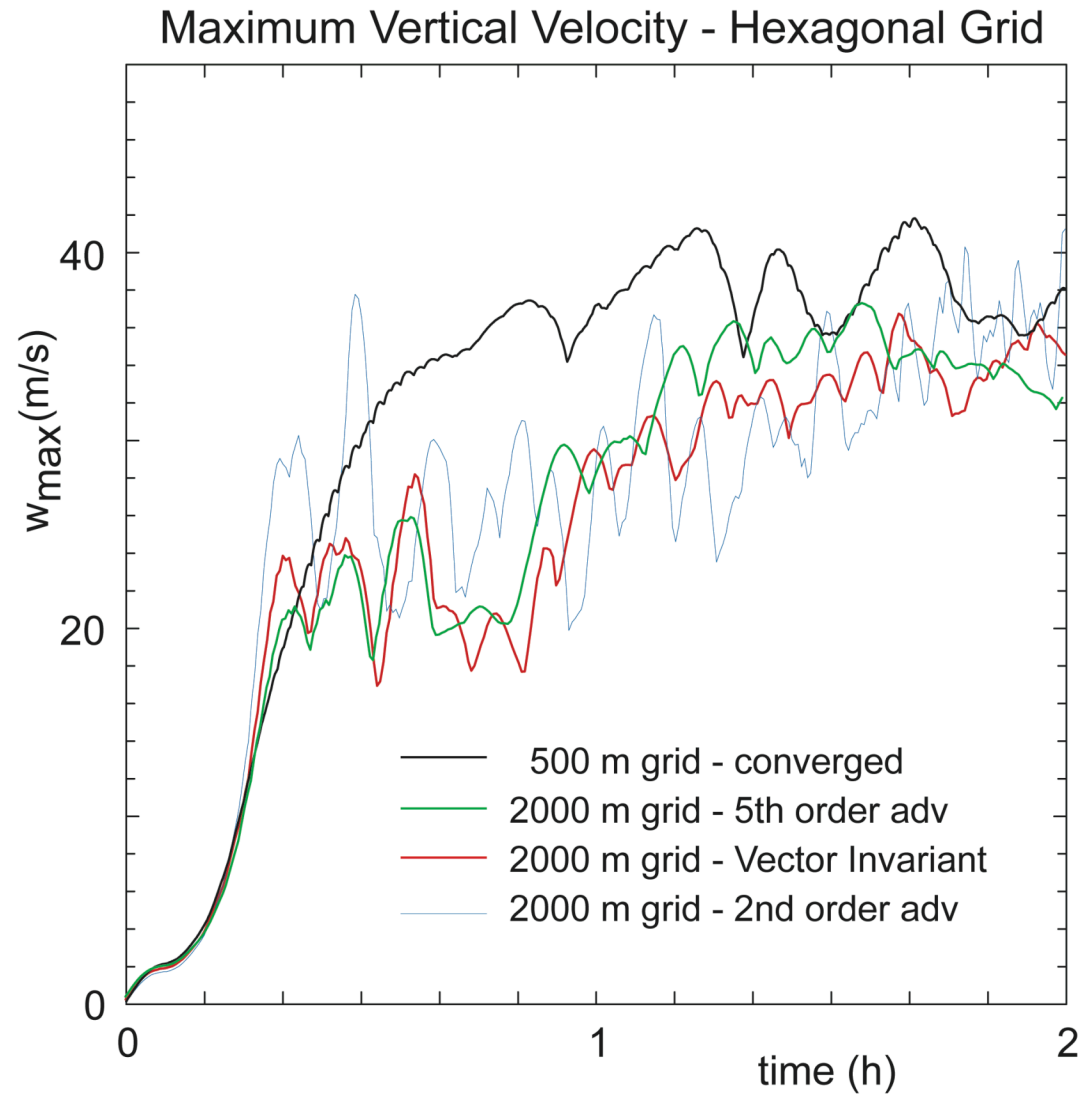
Hexagonal Grid



- Vertical velocity contours at 1, 5, and 10 km (c.i. = 3 m/s)
- 30 m/s vertical velocity surface shaded in red
- Rainwater surfaces shaded as transparent shells
- Perturbation surface temperature shaded on baseplane



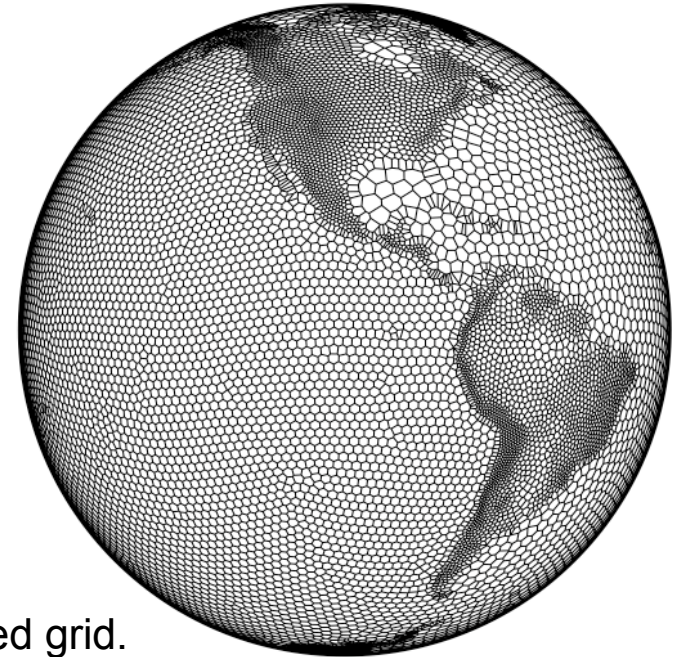
# 3-D Supercell Simulation - Maximum Vertical Velocity



# Summary

## *New SW solver for SVCT C-grid*

- Recovers stationary geostrophic mode.
- Conserves PV to round off.
- Conserves energy to time truncation.
- Solutions comparable to existing SW solvers, and no dissipation needed for standard SW test cases.
- Variable-resolution grid results are encouraging.
- Nonhydrostatic solver as accurate and efficient as existing cloud models
- Parallel SWL solver implemented for an unstructured grid.



## *Next Steps: MPAS development*

- Hydrostatic 3D SVCT solver (based on SW solver).
- Nonhydrostatic solver (based on hydrostatic solver).
- Higher-order transport schemes (Bill Skamarock - next talk).
- Continued variable-resolution grid testing.

