



Implementation of a fully three dimensional advection scheme for the COSMO dynamical core

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- Advection of positive definite quantities
- Scheme used: MPDATA
 - **M**ultidimensional **P**ositive **D**efinite **A**dvection **T**ransport **A**lgorithm developed by P. K. Smolarkiewicz (NCAR) and used in EULAG
- Tests presented (preliminary results):
 - 1d and 2d rotations
- Compared with:
 - **Bott** (2nd order with Strang splitting, operational)
 - **Semi-Lagrange** (3 dimensional scheme)



For more,
questions or discussions ...
see you at the poster!

Thank you!



Agenda

- Advection in COSMO
- Introduction to the **M**ultidimensional **P**ositive **D**efinite **A**dvection **T**ransport **A**lgorithm, MPDATA
- Implementation of MPDATA
- 1 dimensional tests
- 2 dimensional tests
- Summary and Conclusions



Introduction to advection in COSMO

- Prognostic variables
u, v, w, T, pp: with upwind scheme 5th order
- Positive definite variables
qv, qc, qi, qr, qs, qg, tke, density: many choices
 - VanLeer scheme
 - PPM (piecewise parabolic method)
 - Semi-Lagrange scheme (SL)
 - Bott scheme (2nd or 4th order)
- Bott scheme
 - **First** step: advective fluxes multiplied by weighting factor
 - **Second** step: limit fluxes $\Rightarrow$ algorithm is positive definite
 - **Split** scheme: even time steps: xyz, odd time steps: zyx
 - Can lead to oscillations, **can empty a cell**, reduced precision



Introduction to MPDATA (i)

- Aim of the diploma thesis (6 months) was to implement, evaluate and test a fully three-dimensional advection scheme in the COSMO model
- New advection scheme: **MPDATA** (**M**ultidimensional **P**ositive **D**efinite **A**dvection **T**ransport **A**lgorithm)
- Main differences:
 - MPDATA is multidimensional
 - Bott is splitted
 - SL is 3D but not conservative



Introduction to MPDATA (ii)

- Developed by P. K. Smolarkiewicz (NCAR) and used in EULAG
- **Iterative** algorithm:
 - **First** step: Upwind-Approximation – positive definite, only 1st order accurate
 - **Second** step: introduction of corrective advection fluxes, which reduce the truncation error produced by Upwind-Solution
- **Optional** further steps to reduce the truncation errors of previous step (at most 2nd order accuracy)
- **Non-oscillatory option:**
fully monotone (no spurious extremes)

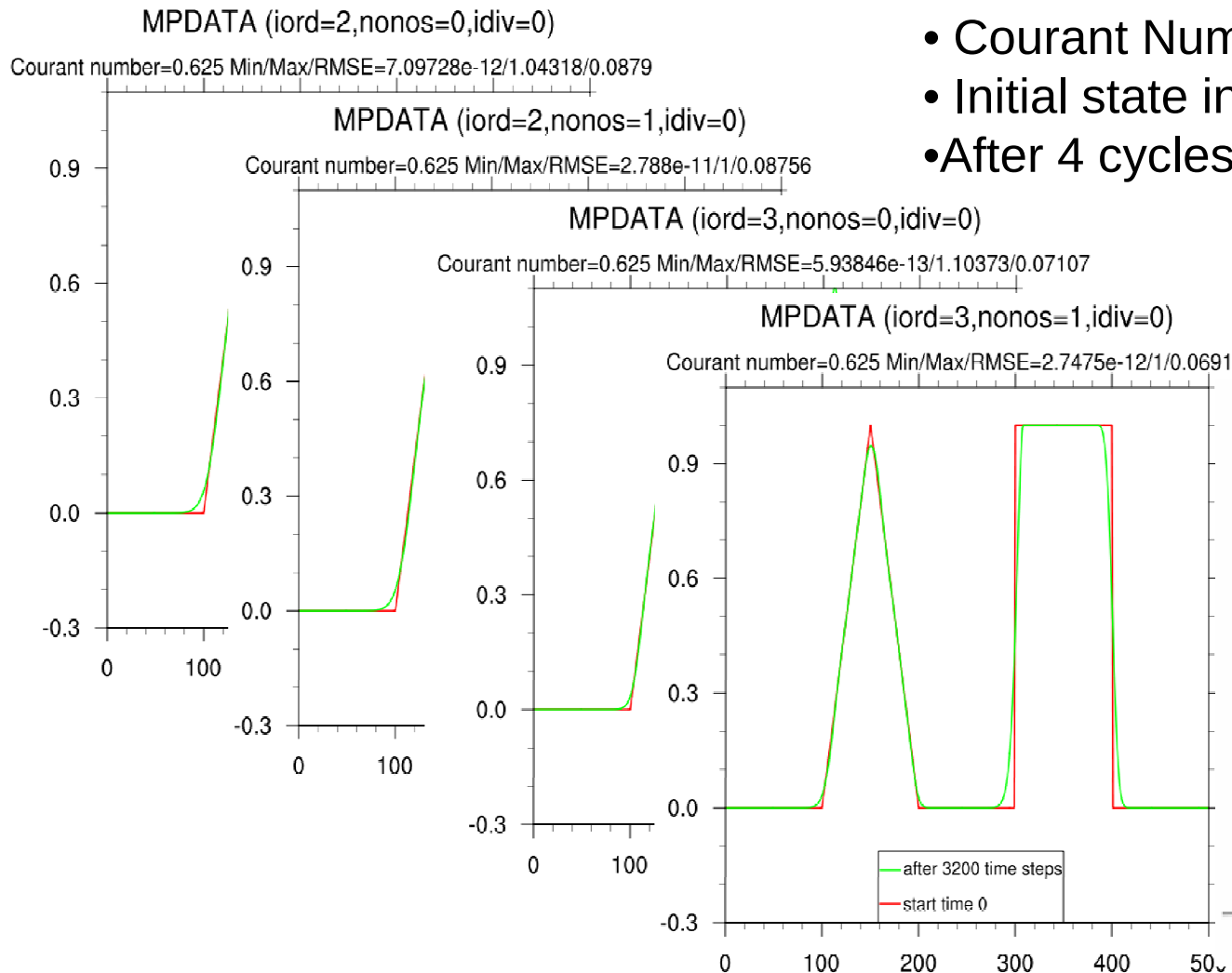


Implementation of MPDATA

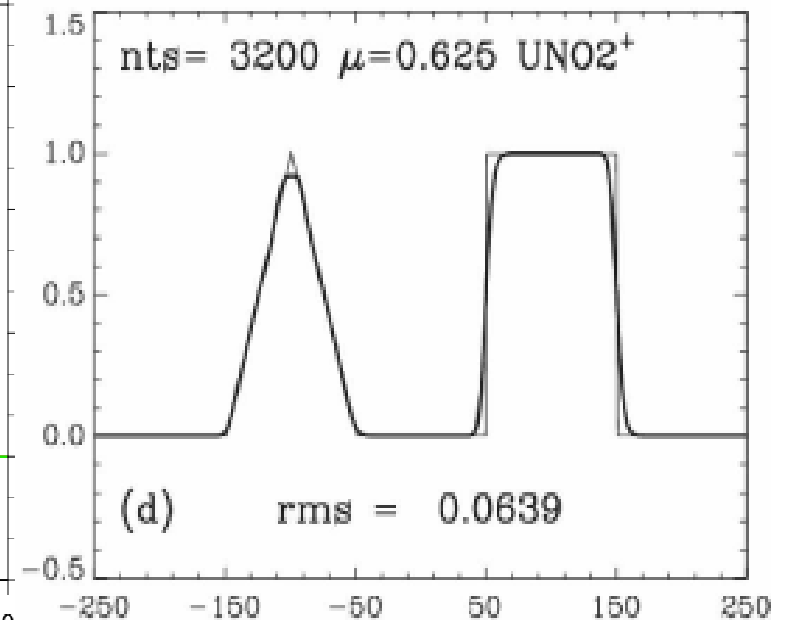
- New Namelist parameters:
 - ***iord***:
 - number of iterations
 - possible values: 1,2,...
 - ***nonos***:
 - nonos=0: non-oscillatory option: off
 - nonos=1: non-oscillatory option: on
(monotone scheme)
 - ***idiv***:
 - idiv=0: non divergent flows
 - idiv=1: divergent flows
- Recommended: iord=2, nonos=1



1-dimensional tests



- Courant Number = 0.625
- Initial state in **red**
- After 4 cycles (+3200 time steps) in **green**

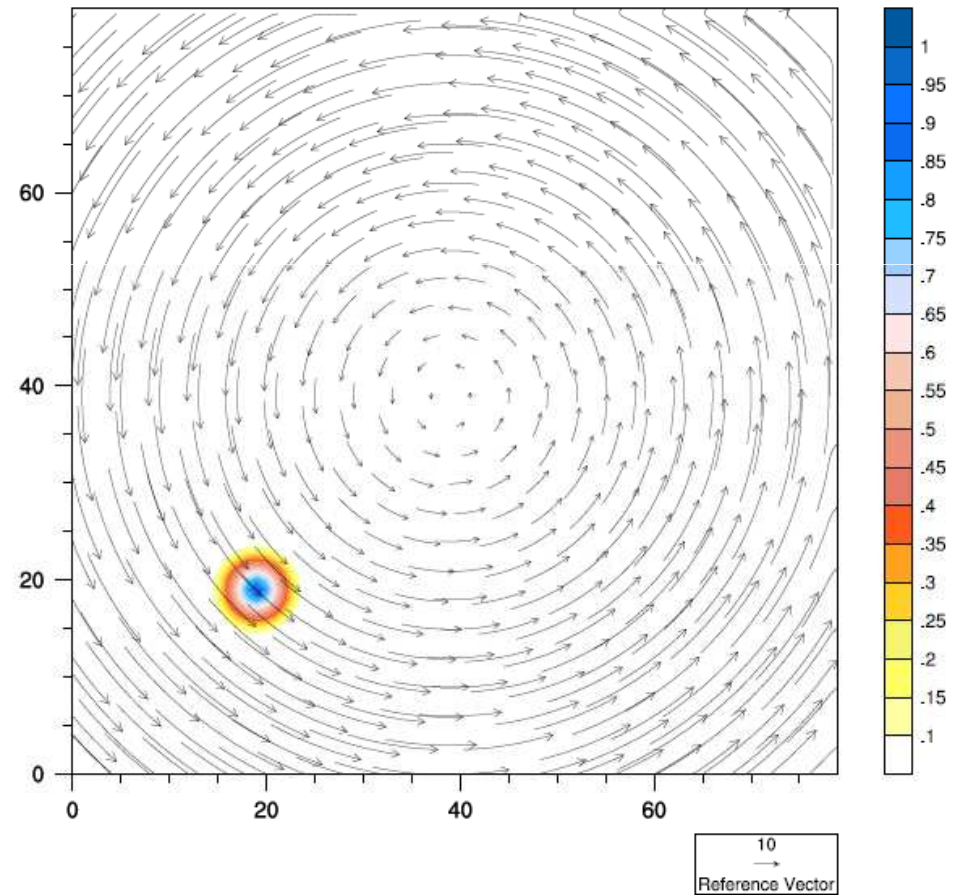


- Upstream Non-Oscillatory scheme from Li (2008)



Solid Body Rotation Tests

- **Cone** tracer with 5 grid points radius
- **NO** background
- **NO** orography
- $\Delta x = 2.2\text{km}$
- $\Delta t = 20\text{s}$
- Courant nb. ~ 0.3



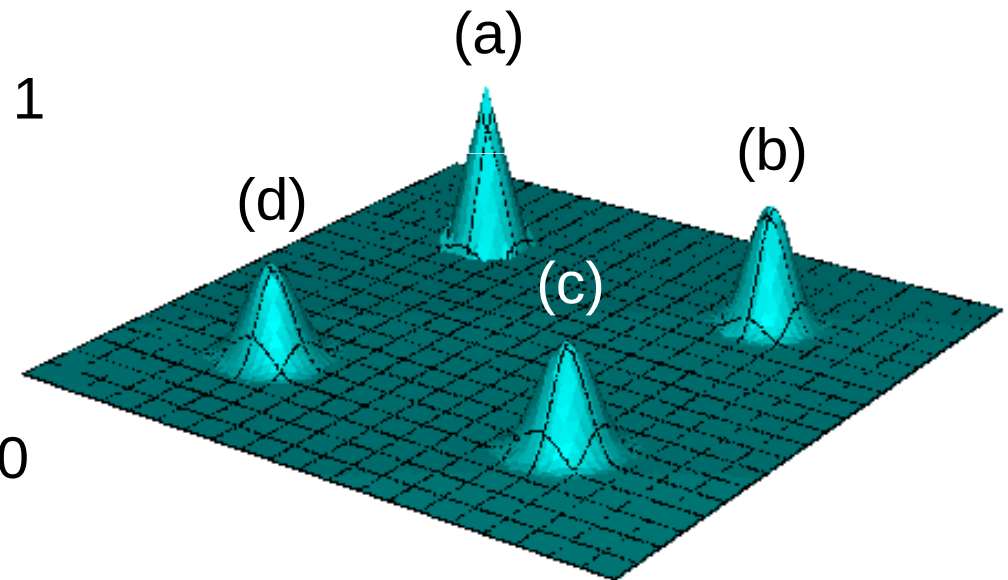
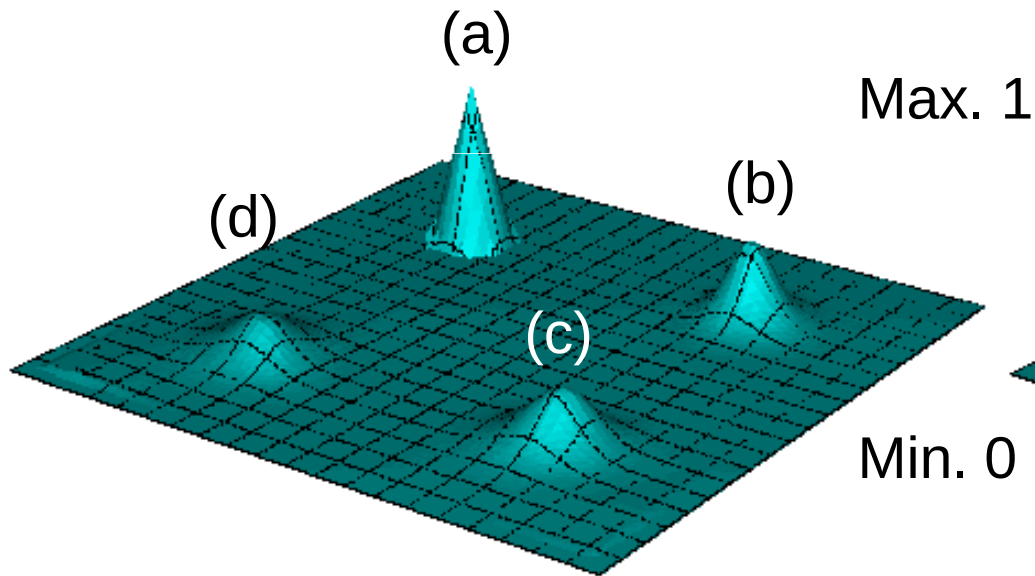
Initial distribution for the solid body rotation tests



Solid Body Rotation Test I

MPDATA (iord=2, nonos=1)

Bott_2 advection scheme



Tracer at the beginning (a), after 1h (b),
after 2h (c) and after 3h (d)



Solid Body Rotation Test I

Zoom of tracer after **one** rotation (4h) (start centre: ✧)

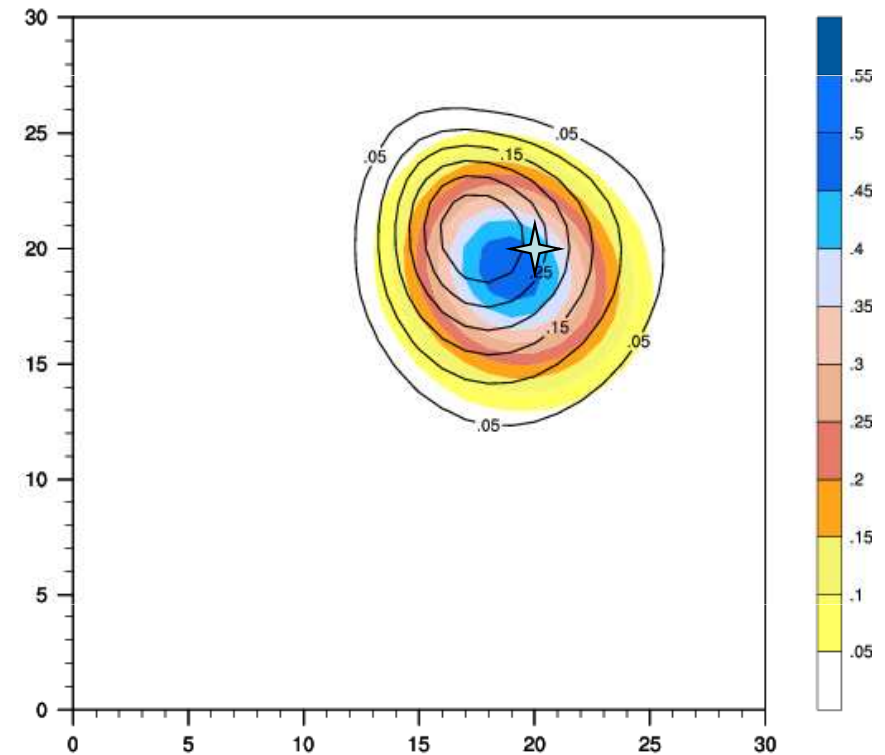
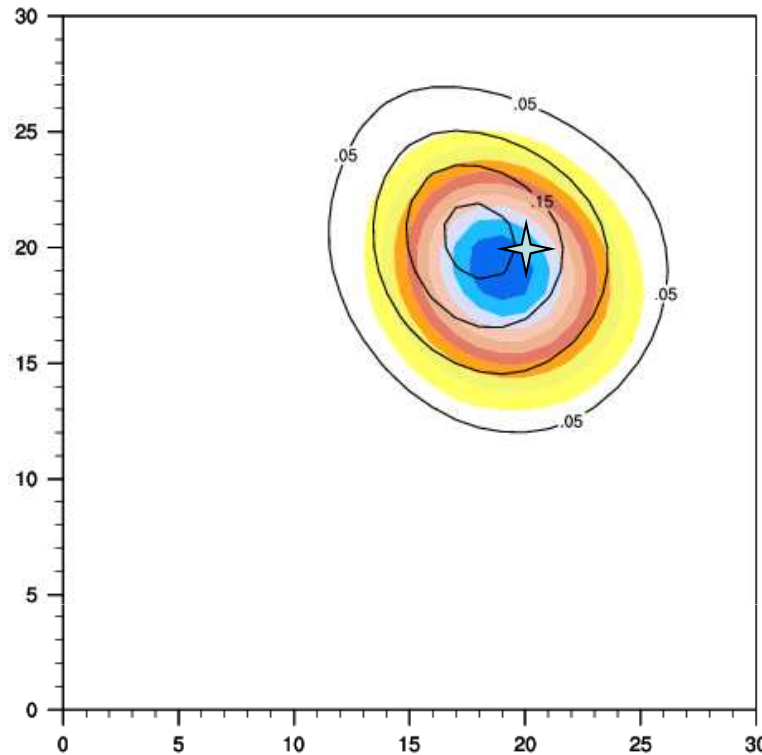
iord=2, nonos=0

Max: 0.2188

Bott Max: 0.5009

iord=3, nonos=0

Max: 0.3480



Bott_2: coloured areas

MPDATA: black contours



Solid Body Rotation Test I

Zoom of tracer after **one** rotation (4h) (start centre: ✧)

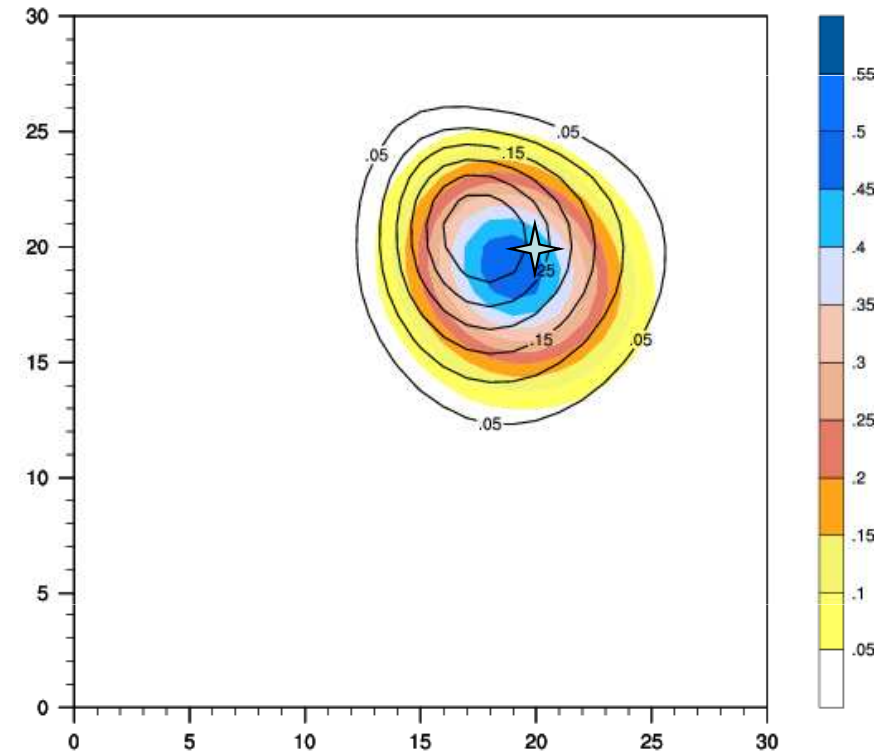
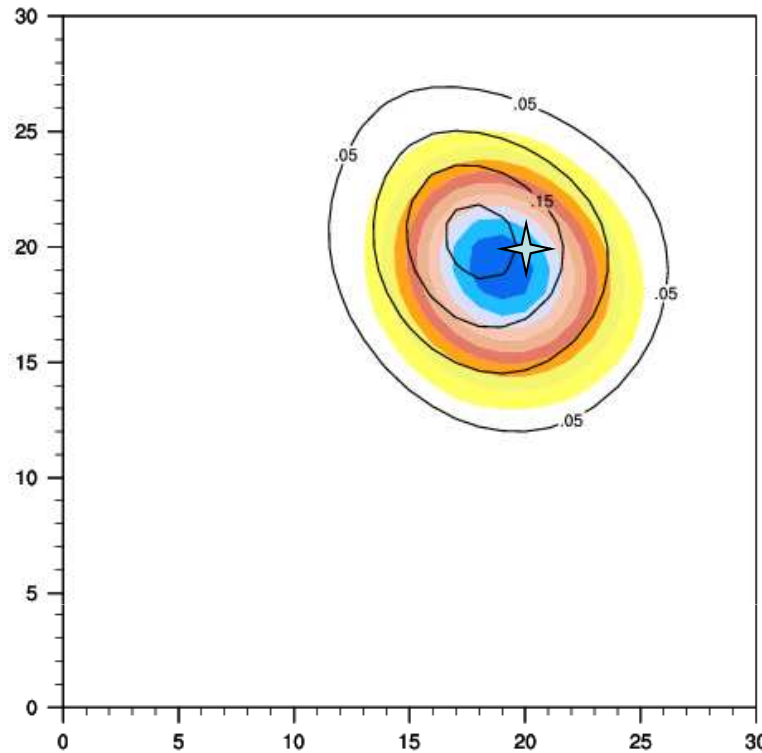
iord=2, nonos=1

Max: 0.2166

Bott Max: 0.5009

iord=3, nonos=1

Max: 0.3439



Bott_2: coloured areas

MPDATA: black contours



Error measures

- **Phase** shift: distance of exact maximum to computed maximum

$$E_{Phase} = \sqrt{(i^{exact} - i^{computed})^2 + (j^{exact} - j^{computed})^2}$$

- **Diffusion**: difference between computed and exact maximum value

$$E_{Diffusion} = \max(qi^{exact}) - \max(qi^{computed})$$



Error measures for Test I

Advection Scheme	Maximum value after one rotation	Phase error	Diffusion error
Bott_2	0.501	1.414	0.499
Semi Lagrange	0.510	1.414	0.490
MPDATA:			
iord=2, nonos=0	0.219	2	0.781
iord=3, nonos=0	0.348	2.236	0.652
iord=2, nonos=1	0.217	2	0.783
iord=3, nonos=1	0.344	2	0.656

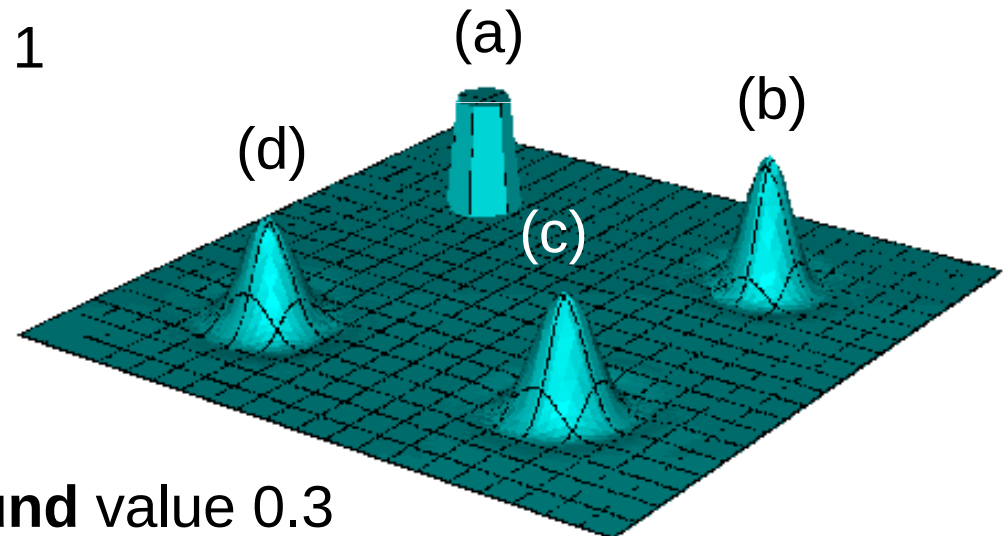
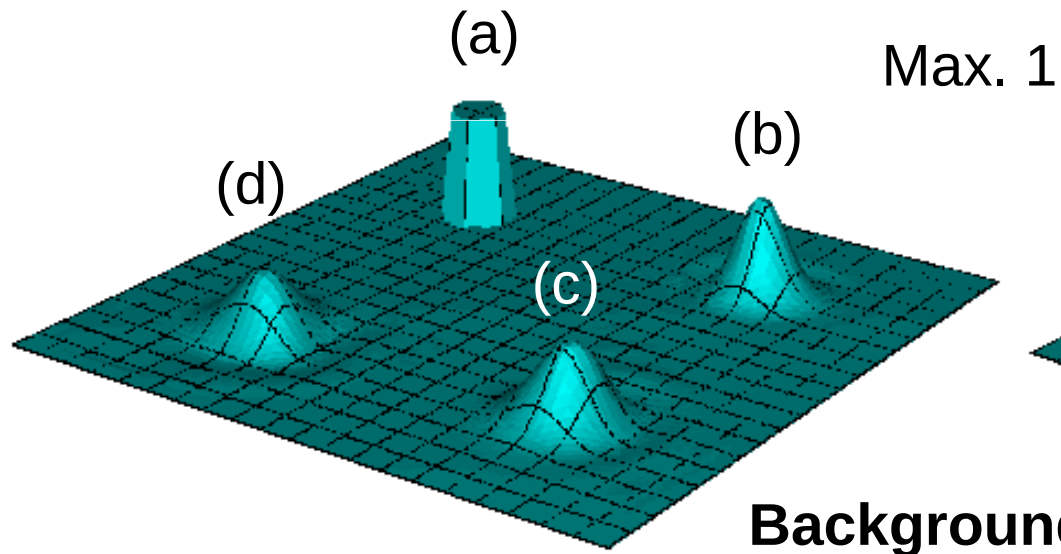
- Conclusions:
- MPDATA is very **diffusive**
 - **large phase errors** for MPDATA
 - **smallest** diffusion error for SL



Solid Body Rotation Test II

MPDATA (iord=2, nonos=1)

Bott_2 advection scheme



Tracer at the beginning (a), after 1h (b),
after 2h (c) and after 3h (d)



Solid Body Rotation Test II

Tracer after **one** rotation (4h) (start centre: )

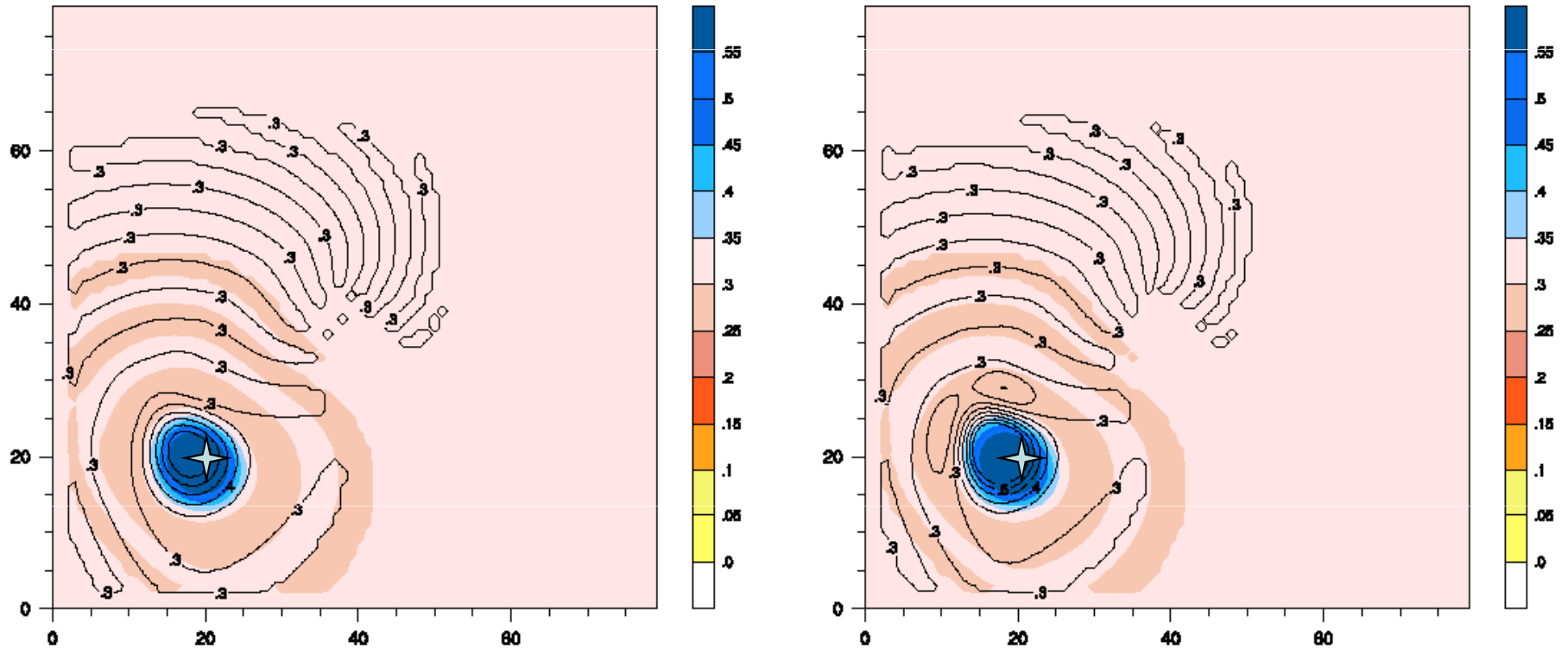
iord=2, nonos=0

Min/Max: 0.2612/0.6333

iord=3, nonos=0

Min/Max: 0.1990/0.7853

Bott Min/Max: 0.2733/0.8439



Bott_2: coloured areas

MPDATA: **black** contours



Solid Body Rotation Test II

Tracer after **one** rotation (4h) (start centre: ✧)

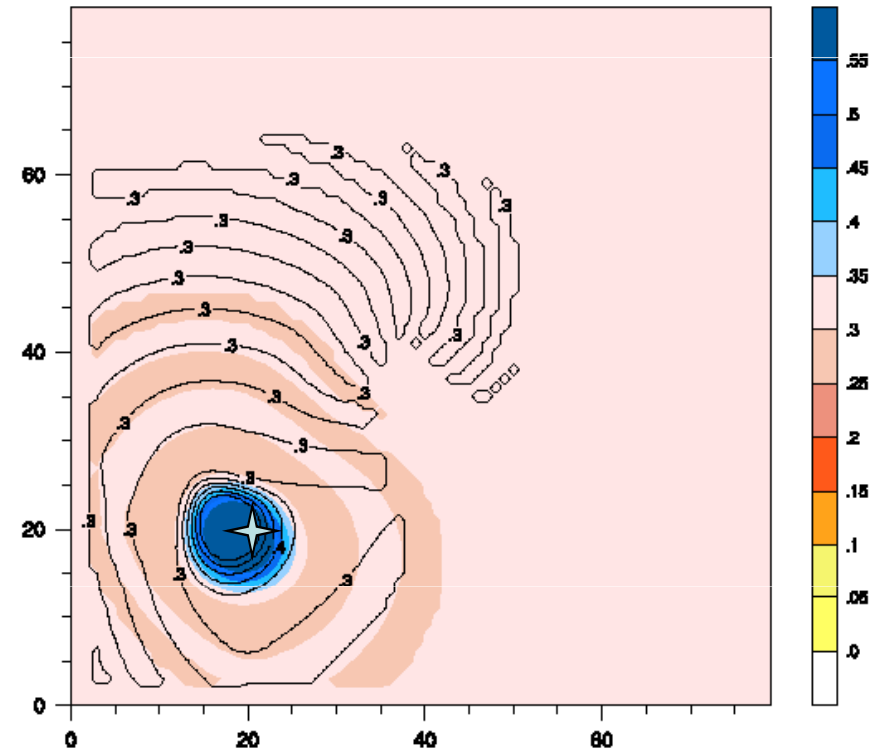
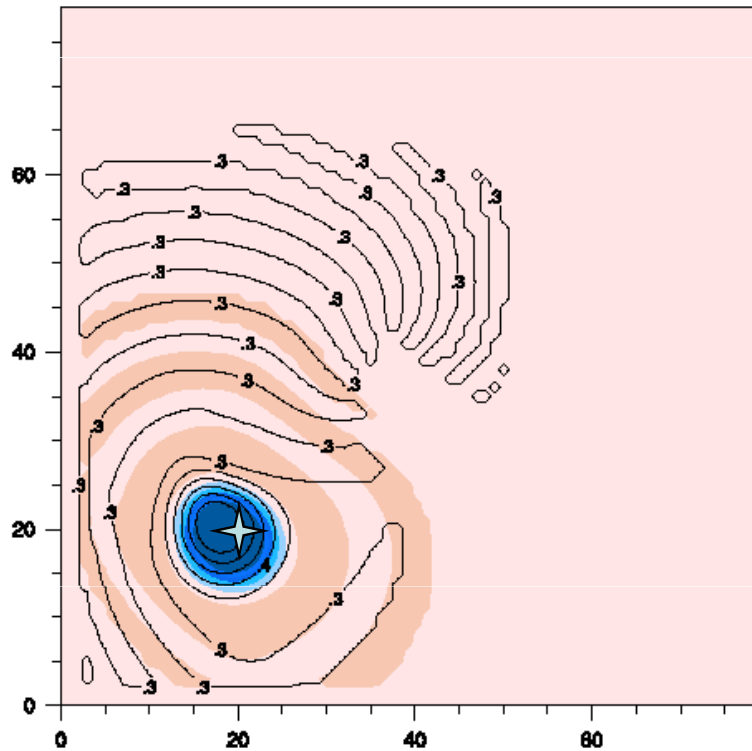
iord=2, nonos=1

Min/Max: 0.2809/0.6249

iord=3, nonos=1

Min/Max: 0.2809/0.7388

Bott Min/Max: 0.2733/0.8439



Bott_2: coloured areas

MPDATA: **black** contours



Error measures for Test II

Advection Scheme	Maximum value after one rotation	Phase error	Diffusion error
Bott_2	0.273 / 0.844	1.414	0.156
Semi Lagrange	0.125 / 0.843	1.414	0.157
MPDATA:			
iord=2, nonos=0	0.261 / 0.633	2	0.367
iord=3, nonos=0	0.199 / 0.785	3.162	0.215
iord=2, nonos=1	0.281 / 0.625	2	0.375
iord=3, nonos=1	0.281 / 0.739	2	0.261

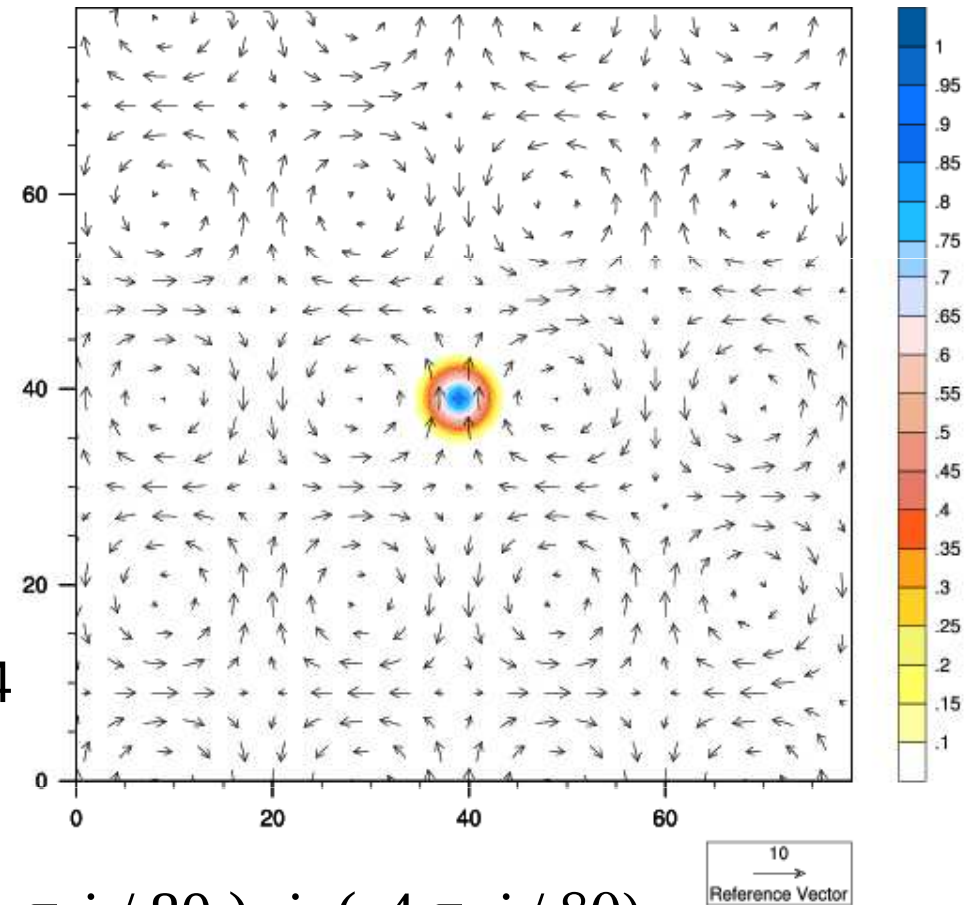
Conclusions:

- **under shooting** of SL (boundary problem)
- **advantage** of the non-oscillatory option of **MPDATA**



Tracer Test in a deformation flow

- **Cone** tracer with 5 grid points radius
- **NO** background
- **NO** orography
- $\Delta x = 2.2\text{km}$
- $\Delta t = 20\text{s}$
- max. Courant nb. ~ 0.04



$$u(i, j) = 120 \pi / 80 \sin(4 \pi i / 80) \sin(4 \pi j / 80)$$

$$v(i, j) = 120 \pi / 80 \cos(4 \pi i / 80) \cos(4 \pi j / 80)$$

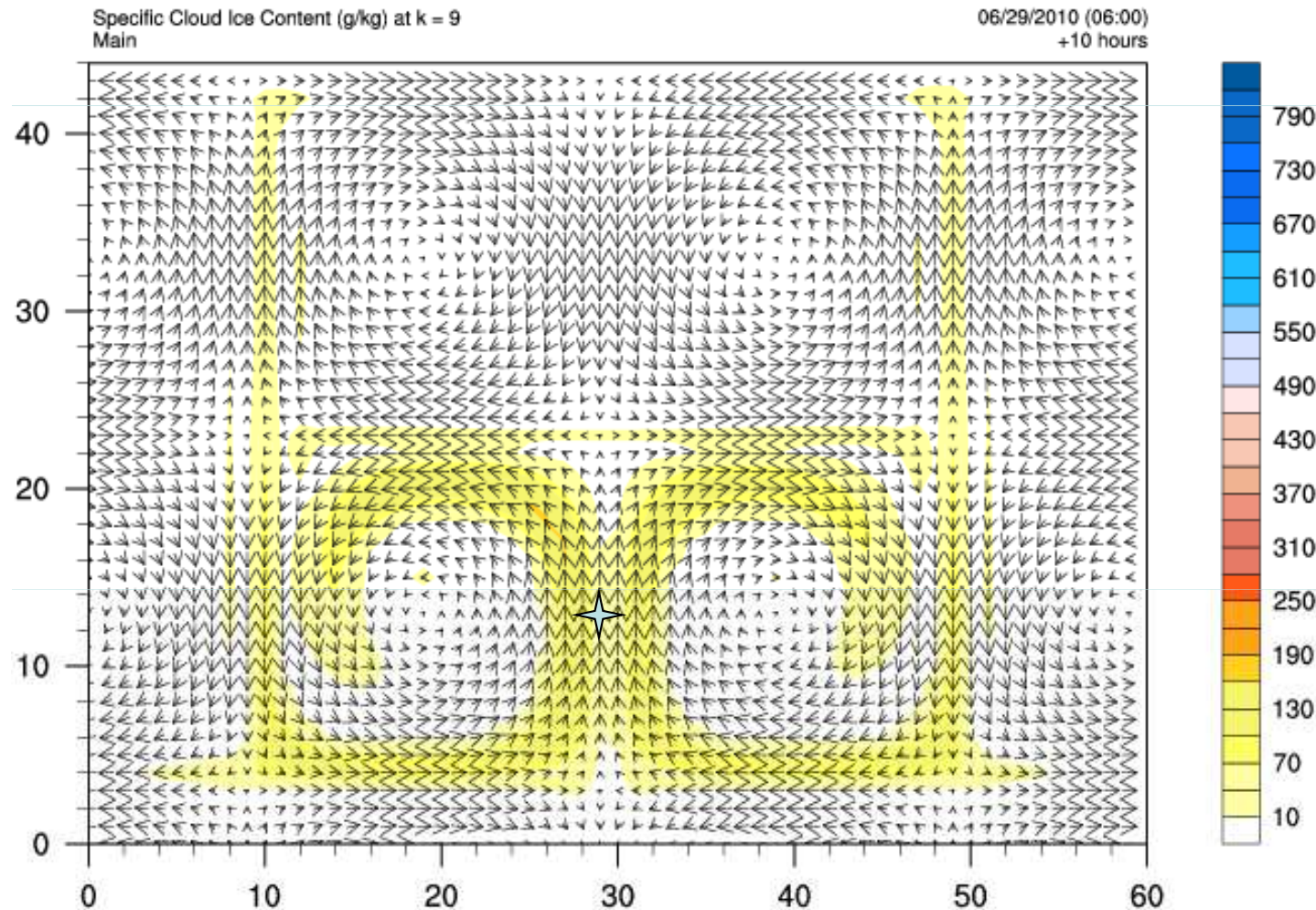


Deformation flow

Zoom of tracer around centre



SL3 Avg: 5.44672g/kg Maximum value: 163.929g/kg



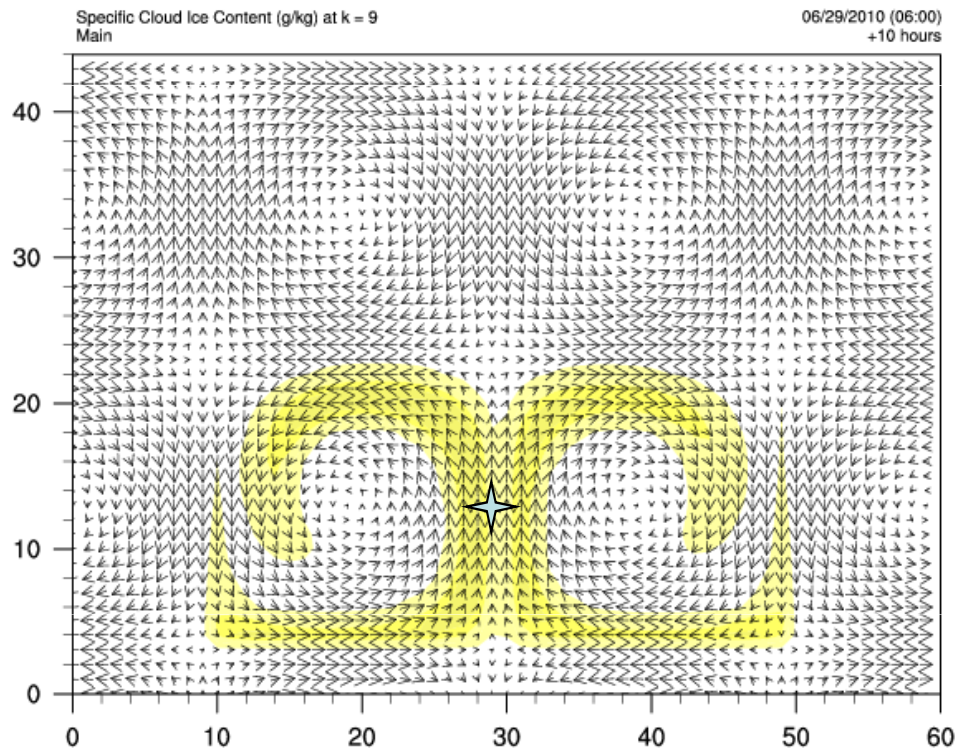


Deformation flow

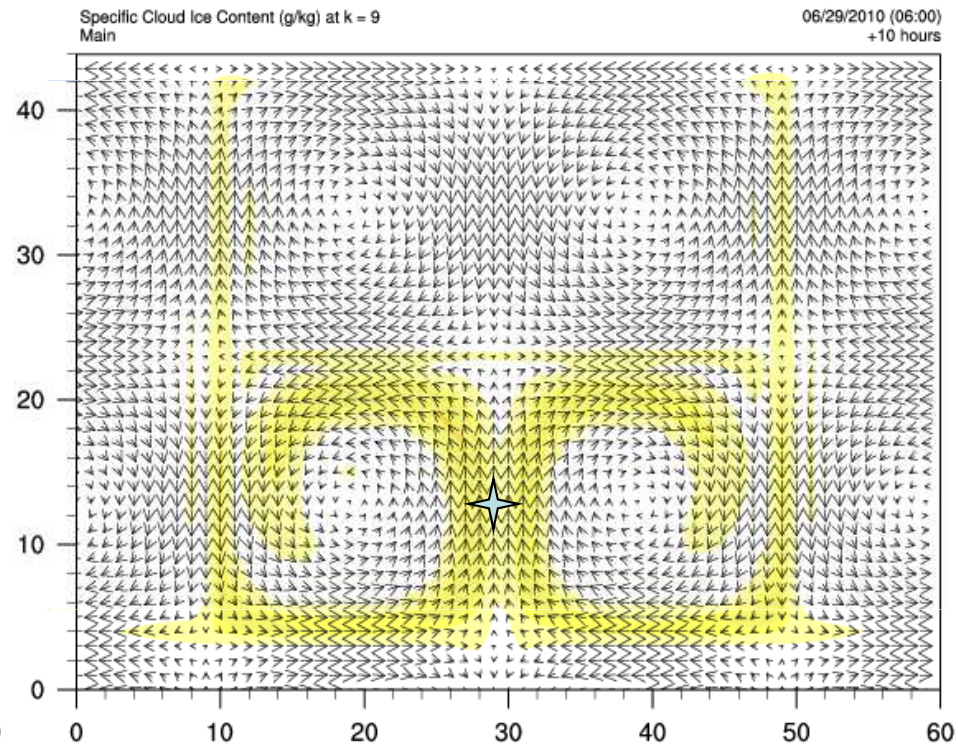
Tracer after 10h (ca. 1.2 rotations) zoom around starting centre ✦

Bott2 Avg: 4.02865g/kg Maximum value: 147.808g/kg

SL3 Avg: 5.44672g/kg Maximum value: 163.929g/kg



Bott_2



Semi-Lagrange

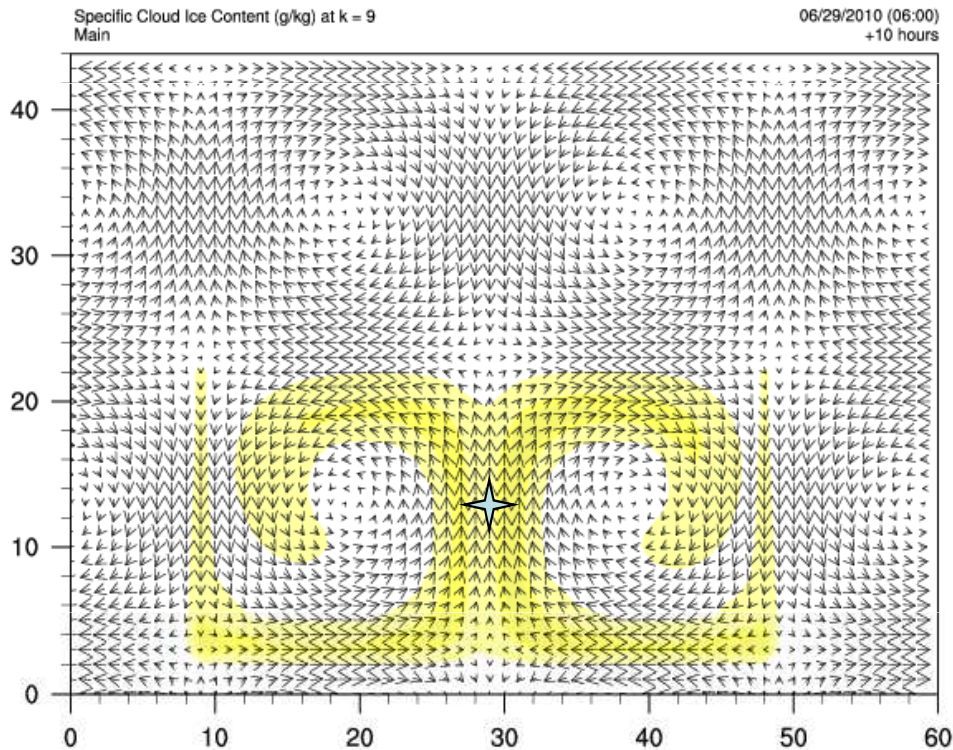


Deformation flow

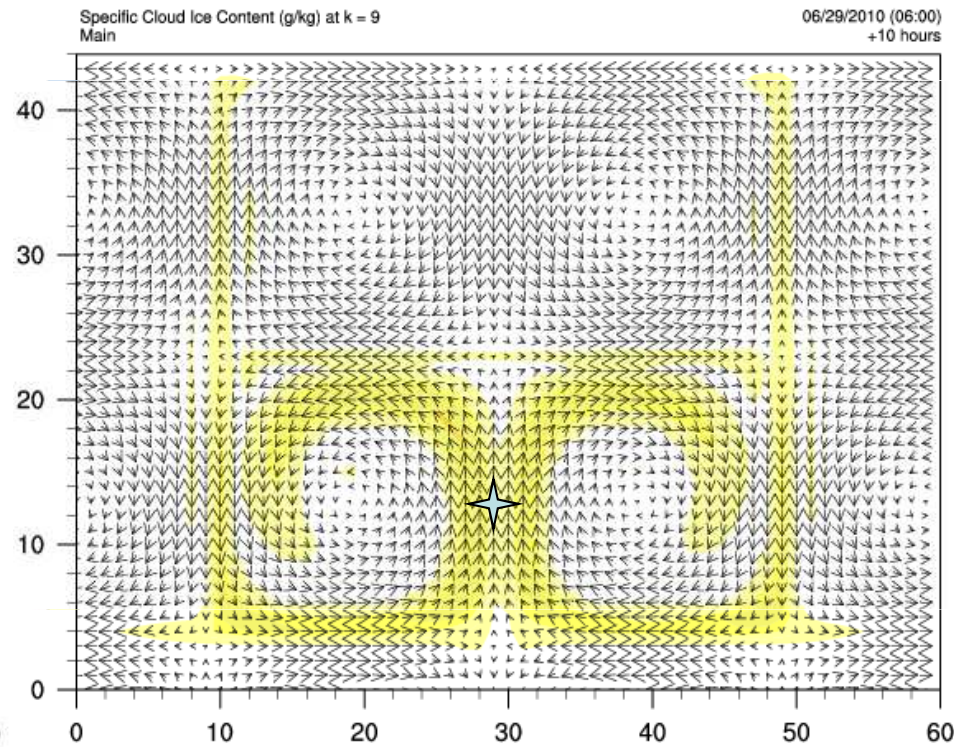
Tracer after 10h (ca. 1.2 rotations) zoom around starting centre ✧

iord3nonos1 Avg: 4.05729g/kg Maximum value: 145.596g/kg

SL3 Avg: 5.44672g/kg Maximum value: 163.929g/kg



iord=3, nonos=1



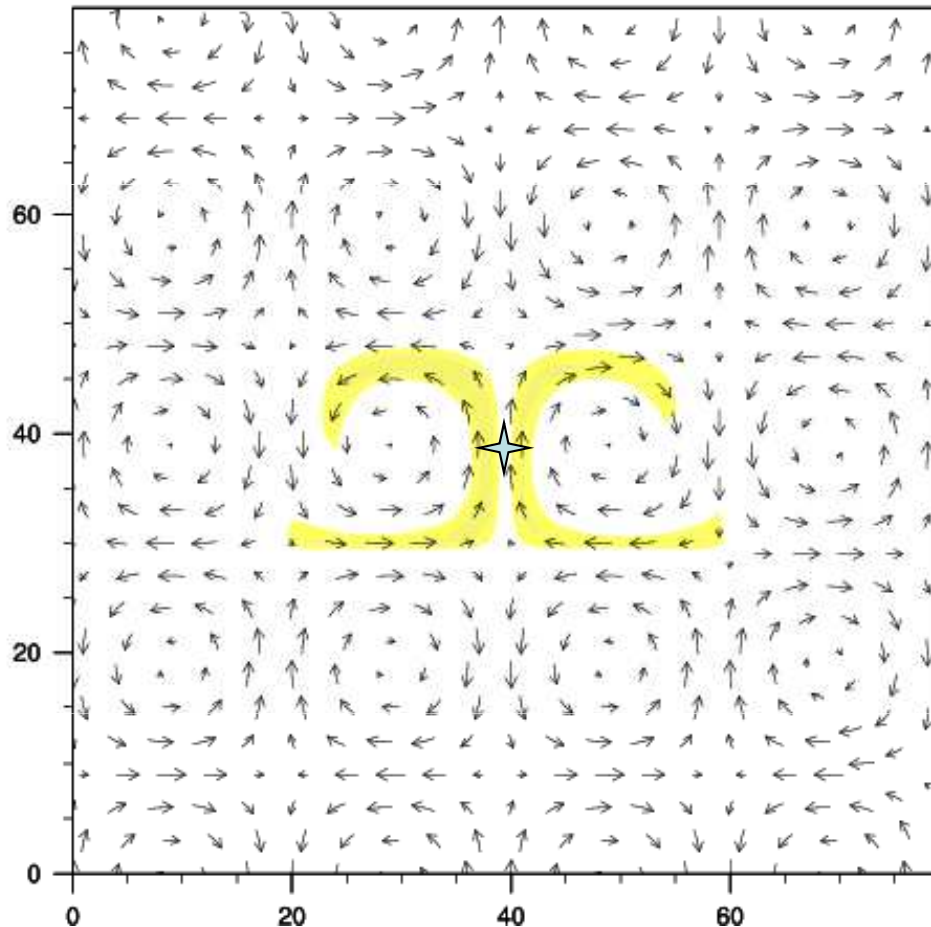
Semi-Lagrange



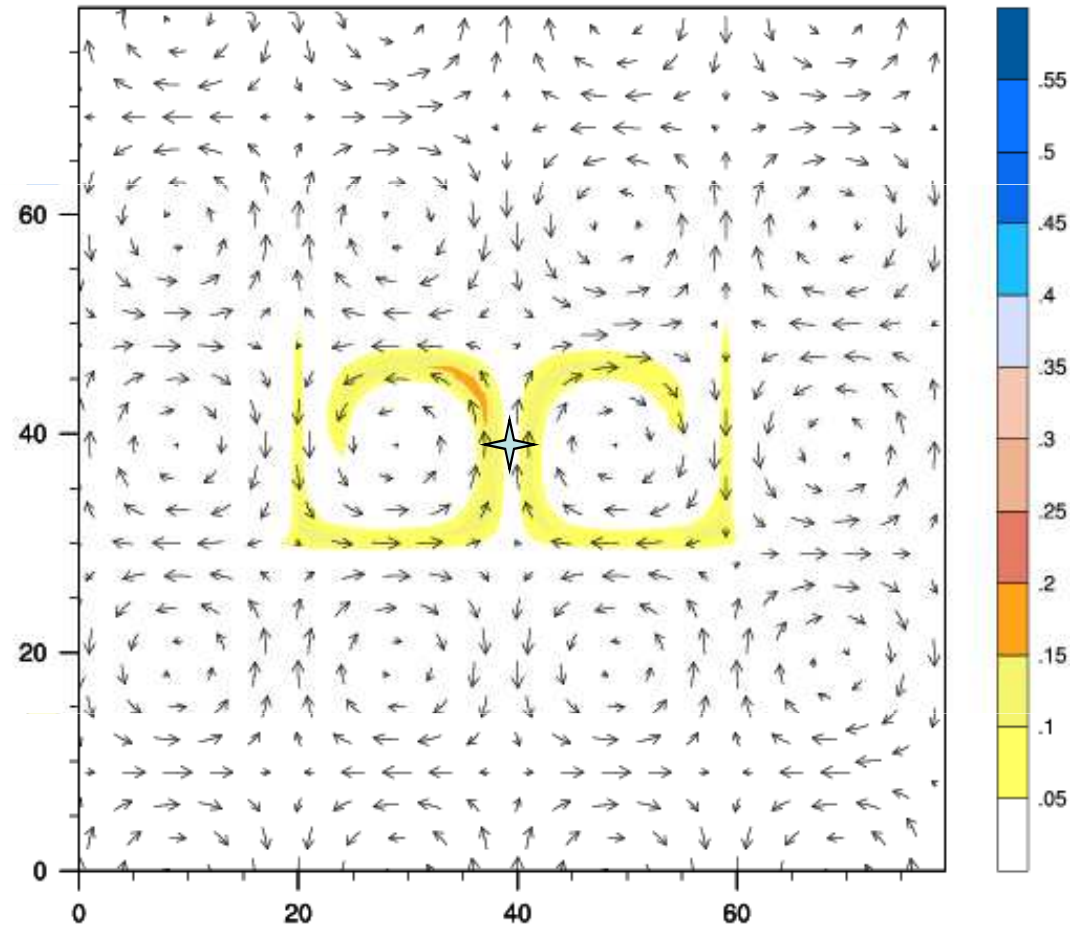
Deformation flow

Tracer after 10h (ca. 1.2 rotations)

start centre: ✧



Bott_2



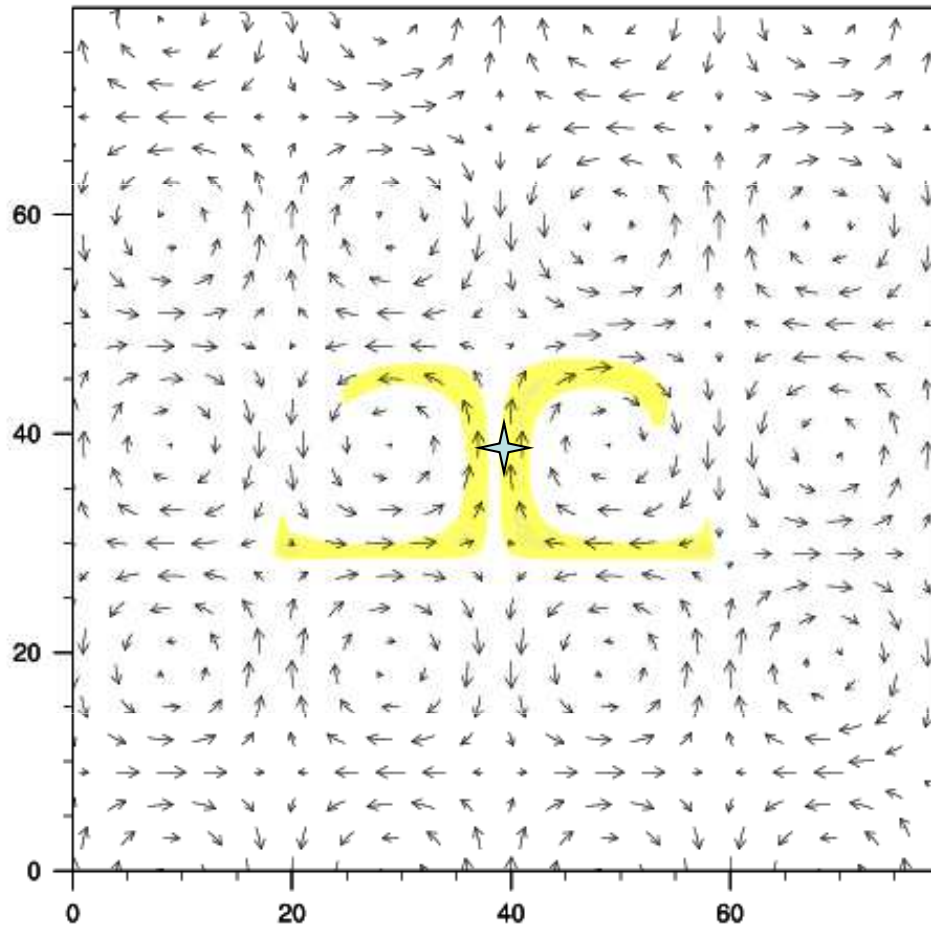
Semi-Lagrange



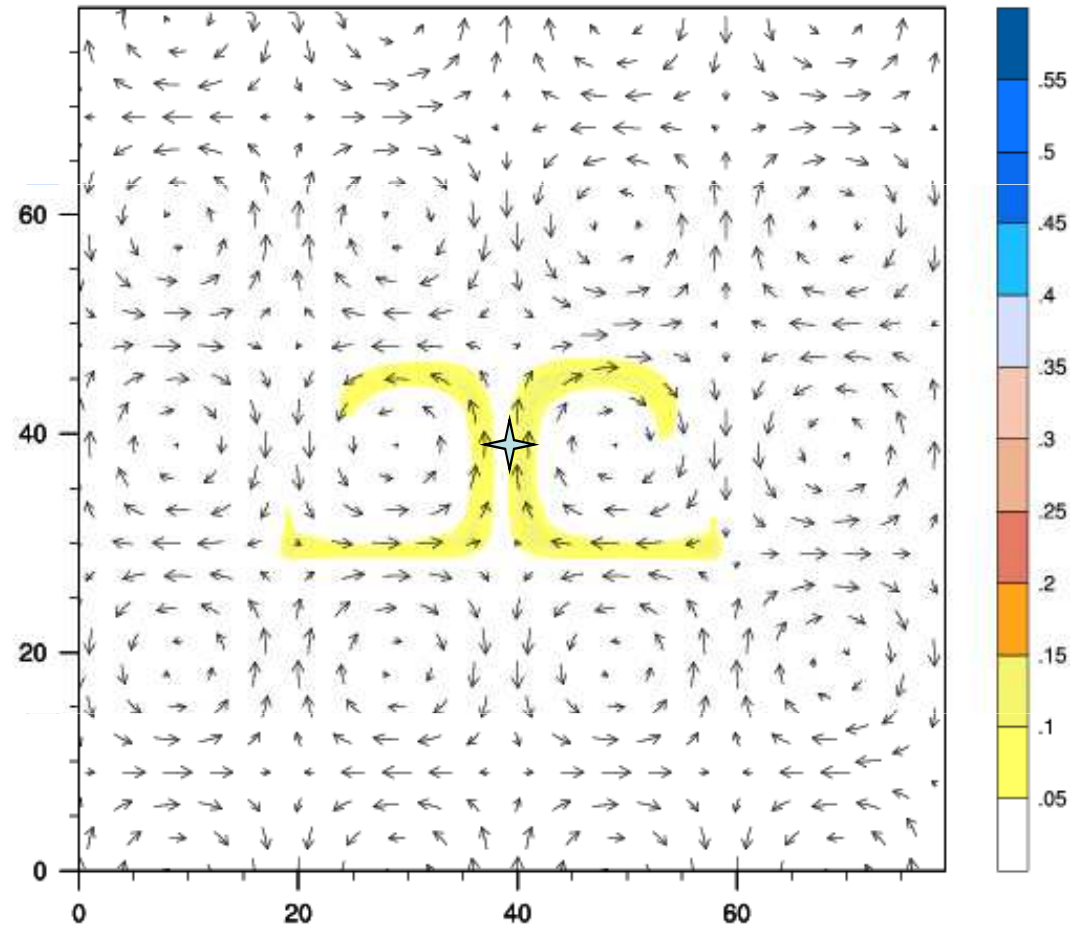
Deformation flow

Tracer after 10h (ca. 1.2 rotations)

start centre: ✧



iord=2, nonos=0



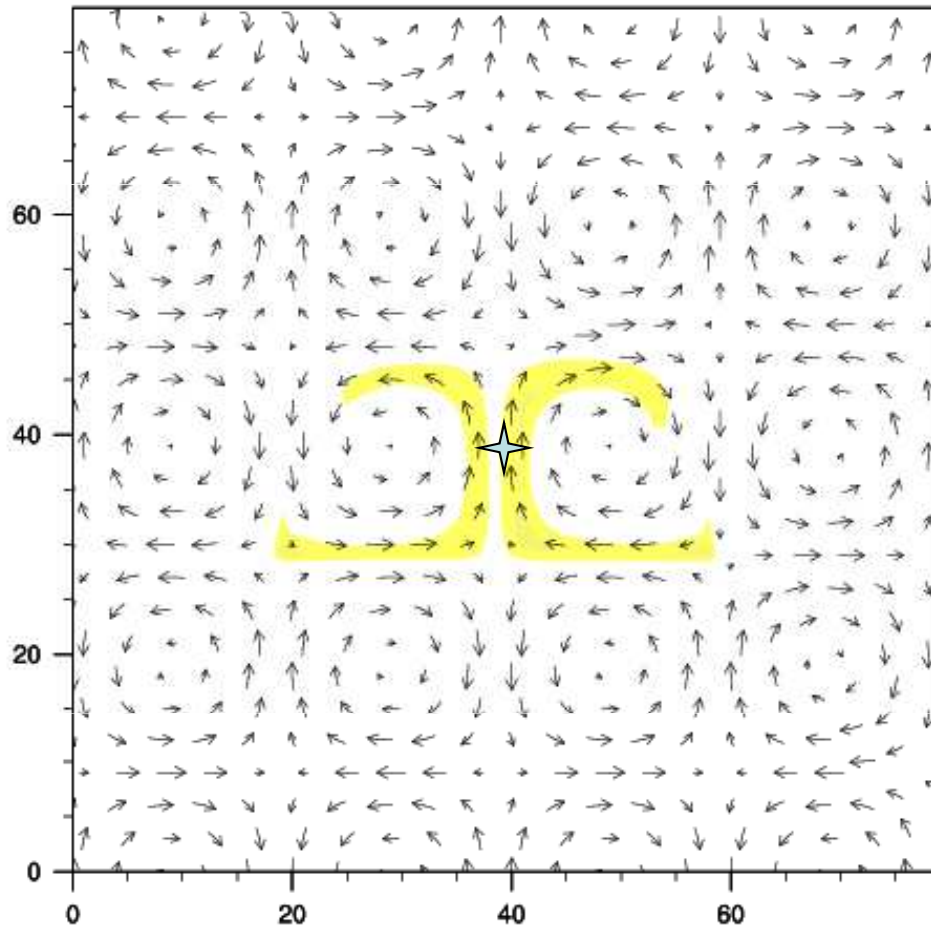
iord=3, nonos=0



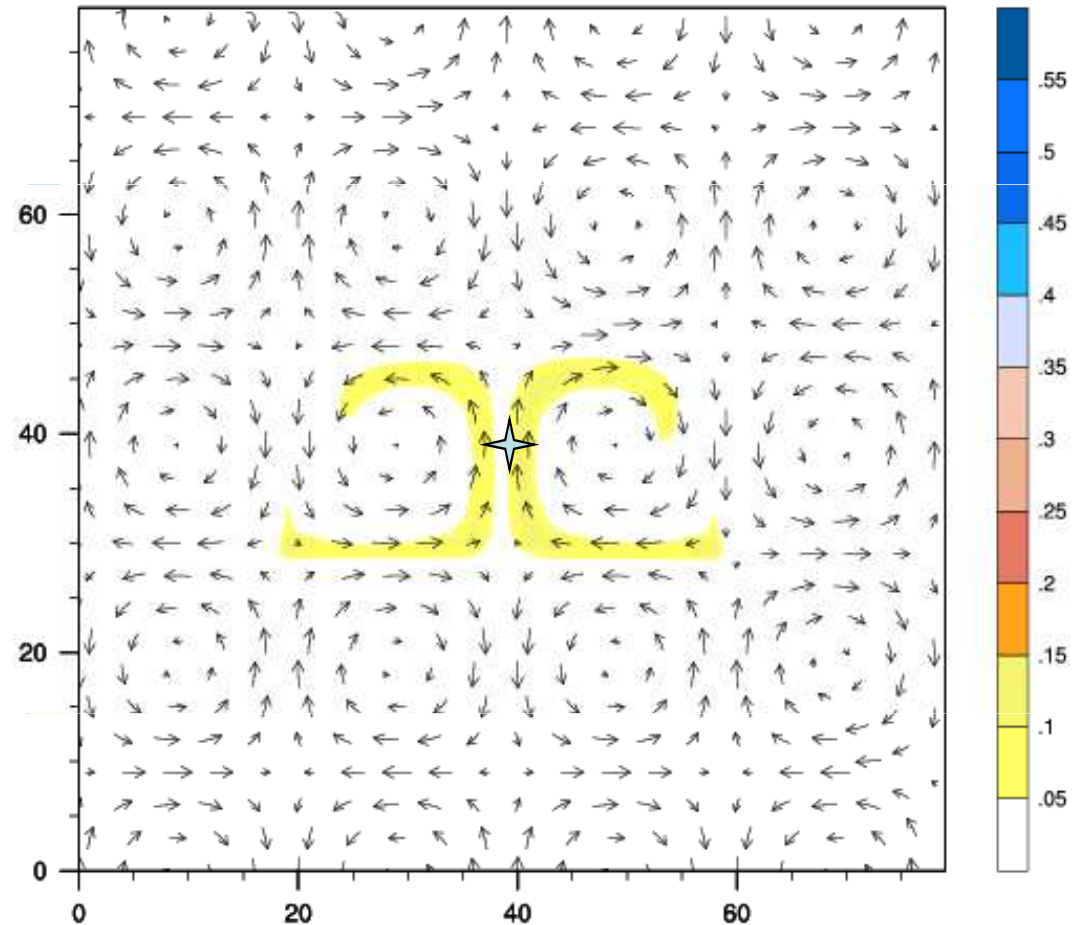
Deformation flow

Tracer after 10h (ca. 1.2 rotations)

start centre: ✧



iord=2, nonos=1



iord=3, nonos=1



Error measures for deformation flow

Advection Scheme	Maximum value after 5h	Maximum value after 10h
Bott_2	0.297	0.148
Semi Lagrange	0.334	0.164
MPDATA:		
iord=2, nonos=0	0.278	0.126
iord=3, nonos=0	0.299	0.149
iord=2, nonos=1	0.267	0.128
iord=3, nonos=1	0.287	0.146

- Conclusions:
- **best** performance for SL
 - **small** impact of MPDATA parameter choice
 - **small** advantage of MPDATA over Bott



Summary and Conclusions

- MPDATA can be much more diffusive than Bott and SL schemes
- High phase errors with MPDATA in rotation tests
- MPDATA is better than the Bott scheme for divergent/convergent flows
- More computer time needed for MPDATA
- MPDATA scheme was not tested in a 3D configuration
- For the moment MPDATA runs only on one processor
- What would the results of Bott with a full strang splitting at each time step (zyxyz) be?



Thank you for your attention!